

PHYSICS 1B – Fall 2007



Electricity & Magnetism



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SERF Building. Room 333

What score do I think I received on the quiz:

- A. 0 out of 10
- B. 1-3 out of 10
- C. 4-6 out of 10
- D. 7-9 out of 10
- E. 10 out of 10

Quiz Grades: Up on 1B website this
week

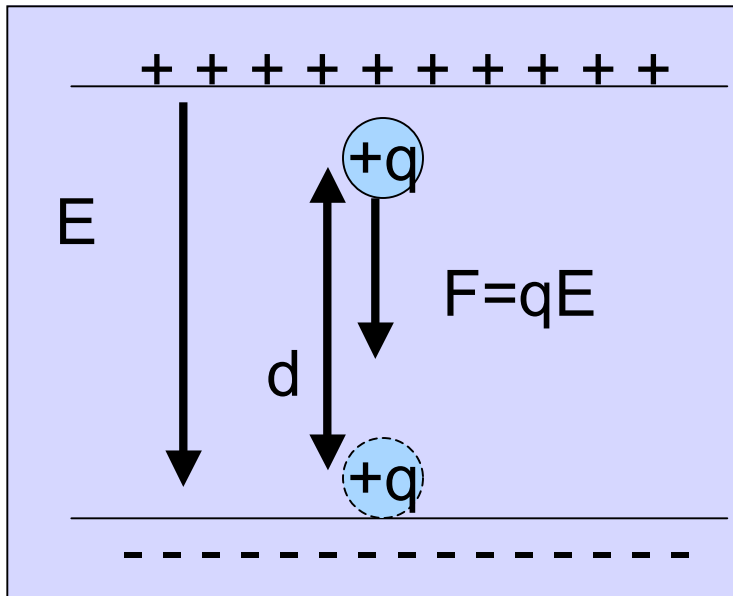


Chapter 16 Electrical Potential

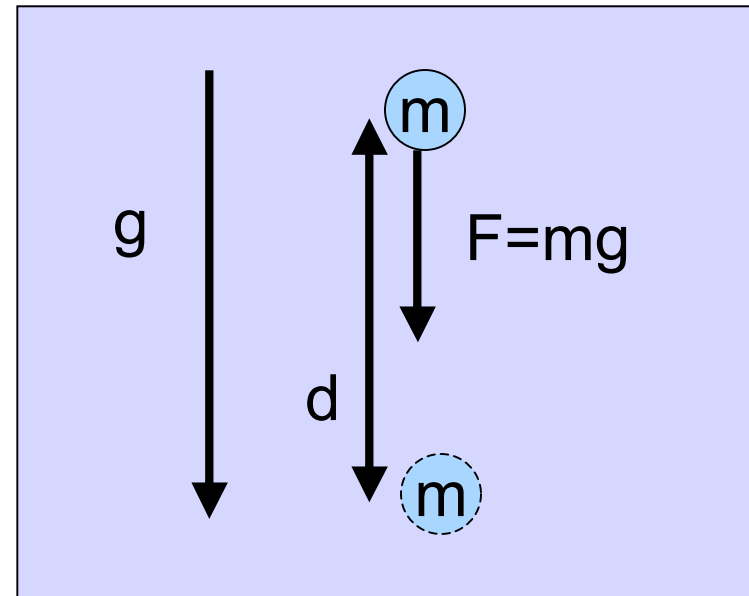
Electrical potential energy

Electrical potential

Potential Energy of a system of charges and masses (the field is uniform, constant)



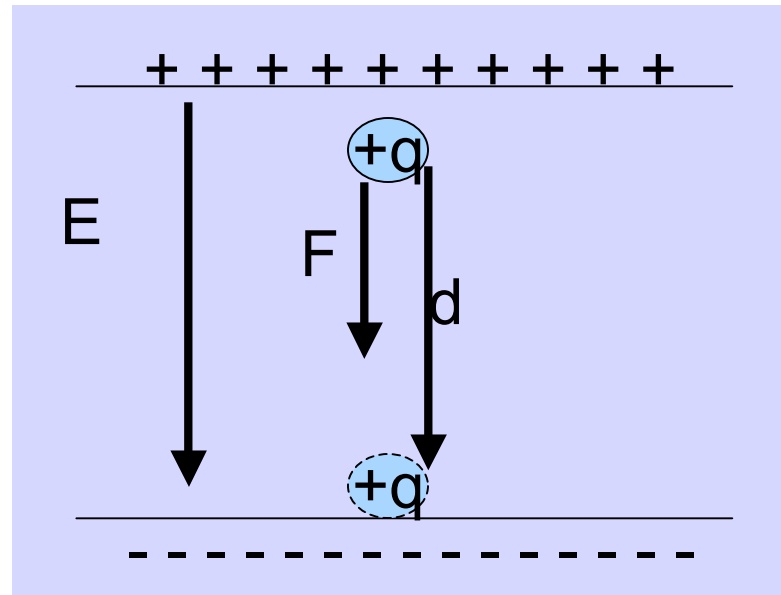
work done by Electric field



work done by Gravitational field

Change in PE = -work done by the field

Potential Energy of a system of charges



$$\Delta PE = -qEd$$

Work done by the Electric field decreases the PE of the system

$$W = Fd$$

$$\Delta PE = -W = -Fd = -qEd$$

Potential, V

$$V = \frac{\Delta PE}{q}$$

Units $\frac{\text{Joules}}{\text{Coulomb}} = \text{Volt (V)}$

Relation between E and V

$$V = Ed$$

$$E = \frac{V}{d}$$

E has units of V/m

Difference between Potential Energy and Potential

Potential-Depends only position in the field.
Units (V)

Potential Energy- Depends on the interaction of the field with a charge. Units (J)

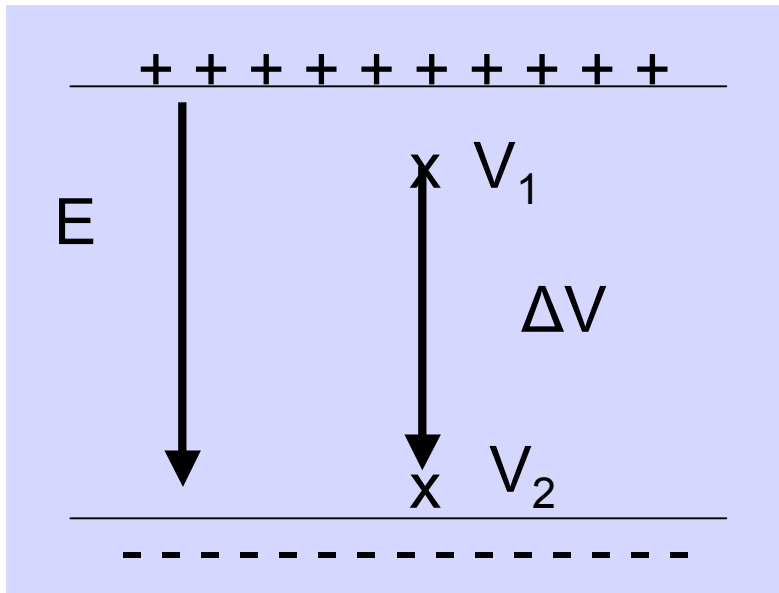
Related by

$$\Delta PE = q\Delta V$$

Both PE and V are relative.

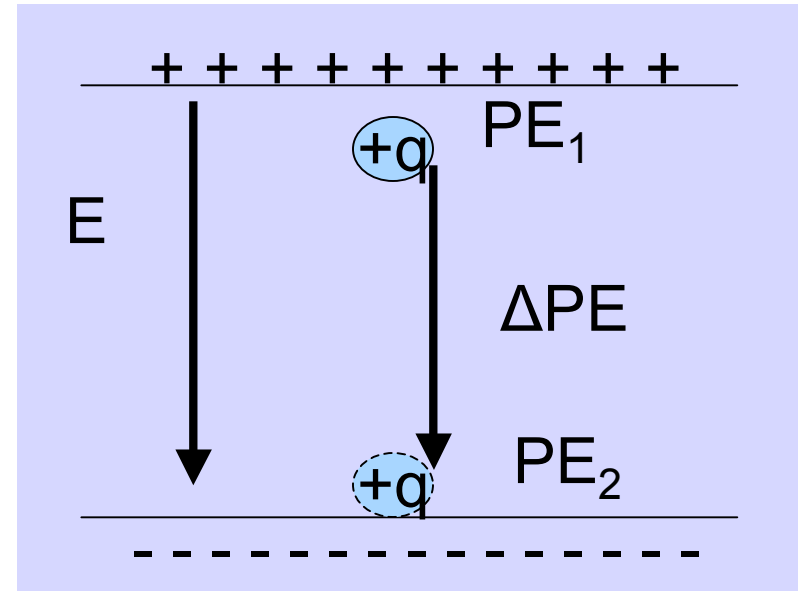
Only differences/changes in Potential Energy and Voltage (ΔPE and ΔV) are important.

Potential



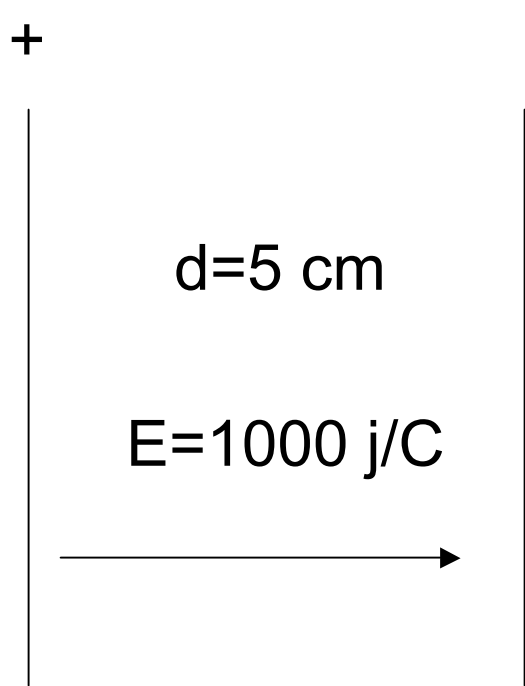
The potential field is a property of the space due to charges

Potential Energy



The potential energy is due to the charge interacting with the potential field.

A parallel plate capacitor has a constant electric field of 1000V/m. The distance between the plates is 5 cm. Find the **potential difference** between the two plates.



$$\Delta V = \frac{\Delta PE}{q} = \frac{qEd}{q} = Ed$$

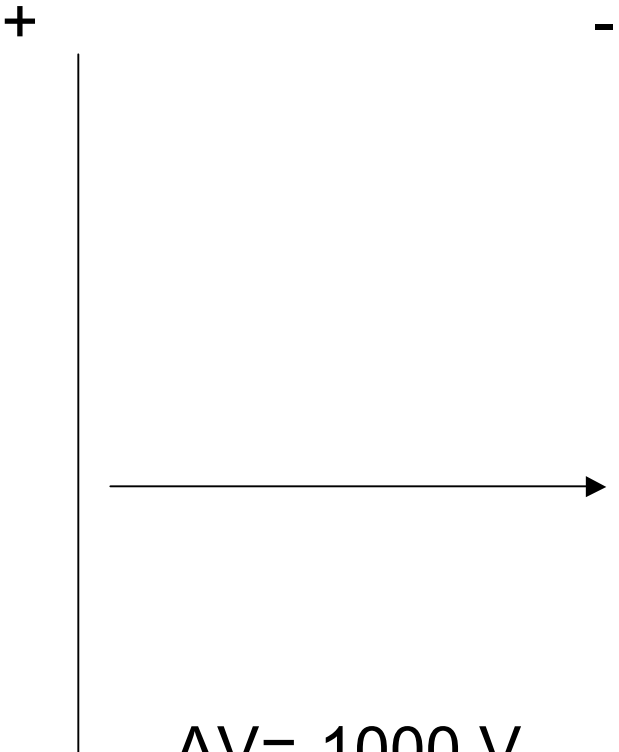
$$\Delta V = 1000(0.05) = 50V$$

Potential Energy = Voltage?

- (T) True
- (F) False



An molecular ion CO^+ is accelerated from rest across a potential difference of 1000 V. Find the final velocity of the ion. Mass= 4.7×10^{-26} kg



$\Delta PE = q\Delta V$

Conservation of Energy

$\Delta PE + \Delta KE = 0$

$\Delta KE = -\Delta PE = -q\Delta V = \frac{1}{2}mv^2$

$v = \sqrt{\frac{2q(-\Delta V)}{m}} = \sqrt{\frac{2(1.6 \times 10^{-19})(1000)}{4.7 \times 10^{-26}}}$

$v = 8.25 \times 10^4 \text{ m/s}$

$\Delta V = -1000 \text{ V}$

Potential due to a point charge

E field is not
constant

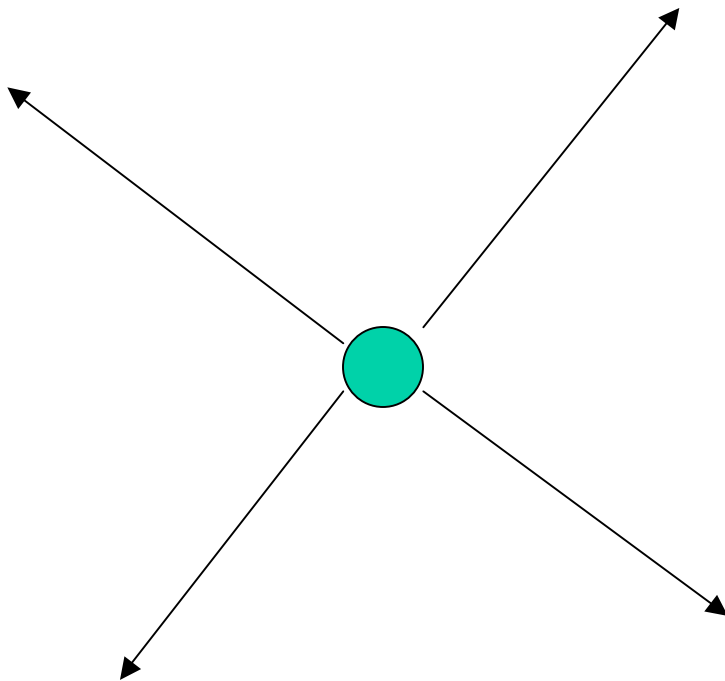
$$E = \frac{k_e q}{r^2}$$

E gets smaller with distance

The potential

$$V = \frac{k_e q}{r}$$

$$V=0 \text{ at } r = \infty$$



Dimensional arguments

V=Electric field x length e.g. for constant field

$$V=Ed$$

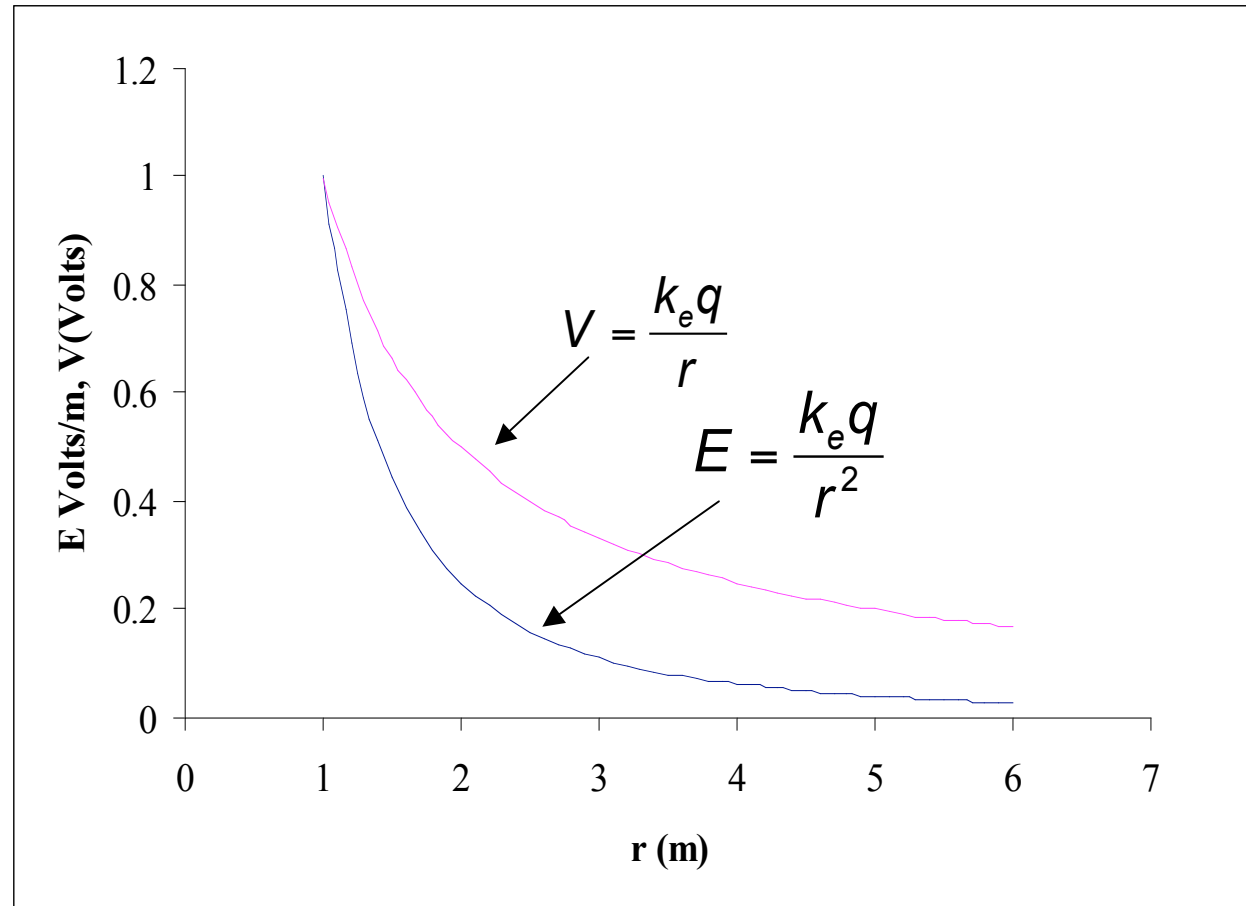
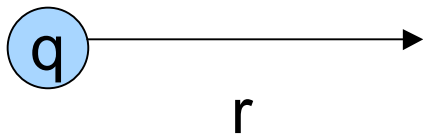
For point charge

$$E = \frac{k_e q}{r^2}$$

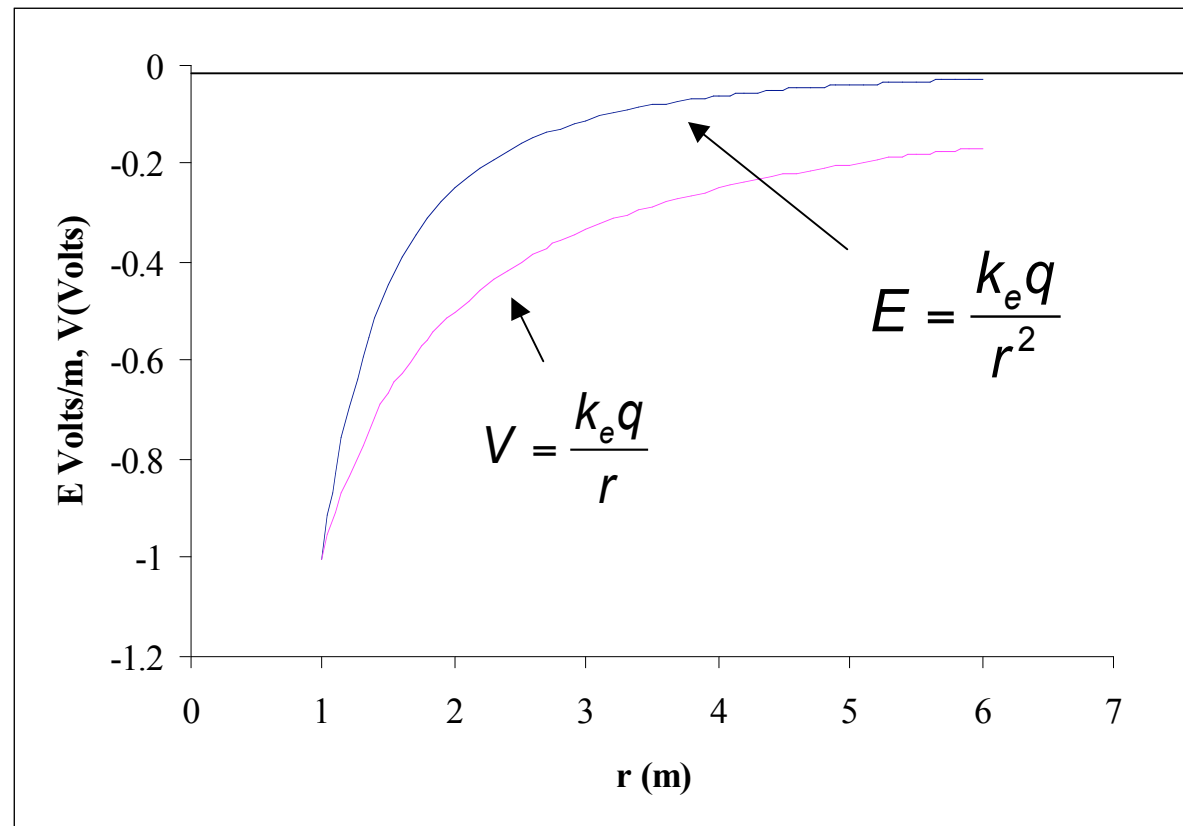
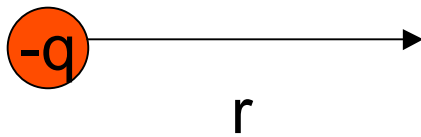
$$V = \frac{k_e q}{r}$$

V has the appropriate units of E times length

Potential and E field due to positive point charge



E and V due to a negative point charge



Potential energy of 2 point charges

$$PE = q_1 V_{21} = q_2 V_{12}$$

V_{21} is the potential due to charge 2 at the position of charge 1.

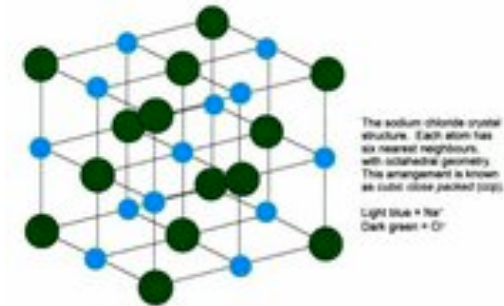
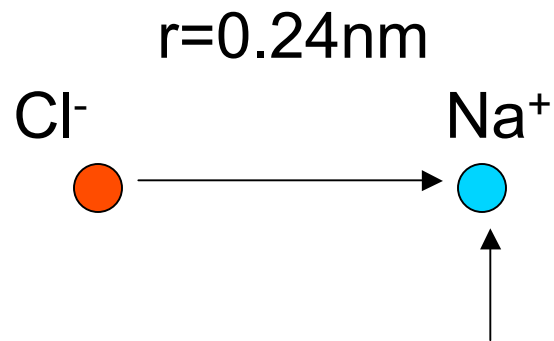


$$PE = \frac{k_e q_1 q_2}{r_{12}}$$

$$PE = 0 \quad \text{at } r = \infty$$

Potential energy and Potential are Scalar
(not Vector) quantities

In a crystal of $\text{Na}^+ \text{Cl}^-$ the distance between the ions is 0.24 nm. Find the potential due to Cl^- at the position of the Na^+ . Find the electrostatic energy of the Na^+ due to the interaction with Cl^- .



$$V = \frac{k_e q}{r} = \frac{9 \times 10^9 (-1.6 \times 10^{-19})}{(0.24 \times 10^{-9})} = -6.0 \text{ V}$$

at the position of Na^+

$$\text{PE} = qV = 1.6 \times 10^{-19} \times -6.0 = -9.6 \times 10^{-19} \text{ J}$$

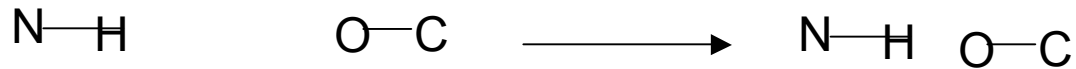
ELECTRON VOLT (convenient unit for atomic physics)

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

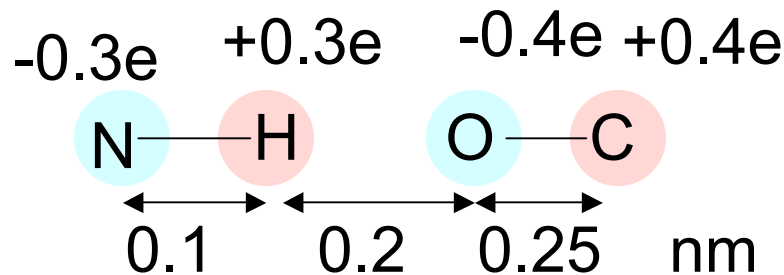
$$\text{PE} = -6.0 \text{ eV}$$

(energy in eV is V times the charge in electron units)

Hydrogen Bond



The hydrogen bond energy can be estimated by partial charges

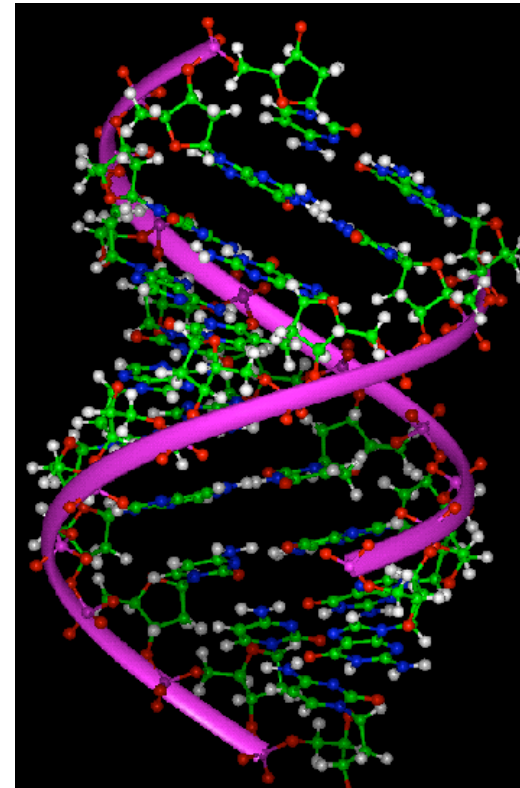


bond energy = sum $\frac{kq_i q_j}{r_{ij}}$ (scalar sum)

$$\Delta\text{PE} = \frac{ke^2}{10^{-9}} \left(\frac{(-.3)(-.4)}{.1+.2} + \frac{-.3(.4)}{.1+.2+.25} + \frac{+.3(-.4)}{.2} + \frac{.3(.4)}{.2+.25} \right) = -3.49 \times 10^{-20} \text{ J}$$

$$\Delta\text{PE} = -0.22 \text{ eV}$$

Weaker than a ionic bond but still significant.



DNA