

Chapter 13

Vibrations and Waves

Answers to Even Numbered Conceptual Questions

4. To understand how we might have anticipated this similarity in speeds, consider sound as a motion of air molecules in a certain direction superimposed on the random, high speed, thermal molecular motions predicted by kinetic theory. Individual molecules experience billions of collisions per second with their neighbors, and as a result, do not travel very far in any appreciable time interval. With this interpretation, the energy of a sound wave is carried as kinetic energy of a molecule and transferred to neighboring molecules by collision. Thus, the energy transmitted by a sound wave in, say, a compression, travels from molecule to molecule at about the rms speed, or actually somewhat less, as observed, since multiple collisions slow the process a bit.
6. Friction. This includes both air-resistance and damping within the spring.
12. The speed of the pulse is $v = \sqrt{F/\mu}$, so increasing the tension F in the hose increases the speed of the pulse. Filling the hose with water increases the mass per unit length μ , and will decrease the speed of the pulse.
16. If the tension remains the same, the speed of a wave on the string does not change. This means, from $v = \lambda f$, that if the frequency is doubled, the wavelength must decrease by a factor of two.
18. The speed of a wave on a string is given by $v = \sqrt{F/\mu}$. This says the speed is independent of the frequency of the wave. Thus, doubling the frequency leaves the speed unaffected.

Problem Solutions

- 13.1 (a) The force exerted on the block by the spring is

$$F_s = -kx = -(160 \text{ N/m})(-0.15 \text{ m}) = +24 \text{ N}$$

or $F_s = \boxed{24 \text{ N directed toward equilibrium position}}$

- (b) From Newton's second law, the acceleration is

$$a = \frac{F_s}{m} = \frac{+24 \text{ N}}{0.40 \text{ kg}} = +60 \frac{\text{m}}{\text{s}^2} = \boxed{60 \frac{\text{m}}{\text{s}^2} \text{ toward equilibrium position}}$$

- 13.15 From conservation of mechanical energy,

$$(KE + PE_g + PE_s)_f = (KE + PE_g + PE_s)_i$$

we have $\frac{1}{2}mv^2 + 0 + \frac{1}{2}kx^2 = 0 + 0 + \frac{1}{2}kA^2$, or $v = \sqrt{\frac{k}{m}(A^2 - x^2)}$

- (a) The speed is a maximum at the equilibrium position, $x = 0$.

$$v_{\text{max}} = \sqrt{\frac{k}{m}A^2} = \sqrt{\frac{(19.6 \text{ N/m})}{(0.40 \text{ kg})}(0.040 \text{ m})^2} = \boxed{0.28 \text{ m/s}}$$

- (b) When $x = -0.015 \text{ m}$,

$$v = \sqrt{\frac{(19.6 \text{ N/m})}{(0.40 \text{ kg})}[(0.040 \text{ m})^2 - (-0.015 \text{ m})^2]} = \boxed{0.26 \text{ m/s}}$$

- (c) When $x = +0.015 \text{ m}$,

$$v = \sqrt{\frac{(19.6 \text{ N/m})}{(0.40 \text{ kg})}[(0.040 \text{ m})^2 - (+0.015 \text{ m})^2]} = \boxed{0.26 \text{ m/s}}$$

- (d) If $v = \frac{1}{2}v_{\text{max}}$, then $\sqrt{\frac{k}{m}(A^2 - x^2)} = \frac{1}{2}\sqrt{\frac{k}{m}A^2}$

This gives $A^2 - x^2 = \frac{A^2}{4}$, or $x = A \frac{\sqrt{3}}{2} = (4.0 \text{ cm}) \frac{\sqrt{3}}{2} = \boxed{3.5 \text{ cm}}$

- 13.19** (a) The motion is simple harmonic because the tire is rotating with constant velocity and you are looking at the uniform circular motion of the “bump” projected on a plane perpendicular to the tire.
- (b) Note that the tangential speed of a point on the rim of a rolling tire is the same as the translational speed of the axle. Thus, $v_t = v_{\text{car}} = 3.00 \text{ m/s}$ and the angular velocity of the tire is

$$\omega = \frac{v_t}{r} = \frac{3.00 \text{ m/s}}{0.300 \text{ m}} = 10.0 \text{ rad/s}$$

Therefore, the period of the motion is

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{10.0 \text{ rad/s}} = \boxed{0.628 \text{ s}}$$

- 13.25** (a) The period of oscillation is $T = 2\pi\sqrt{m/k}$ where k is the spring constant and m is the mass of the object attached to the end of the spring. Hence,

$$T = 2\pi\sqrt{\frac{0.250 \text{ kg}}{9.5 \text{ N/m}}} = \boxed{1.0 \text{ s}}$$

- (b) If the cart is released from rest when it is 4.5 cm from the equilibrium position, the amplitude of oscillation will be $A = 4.5 \text{ cm} = 4.5 \times 10^{-2} \text{ m}$. The maximum speed is then given by

$$v_{\text{max}} = A\omega = A\sqrt{\frac{k}{m}} = (4.5 \times 10^{-2} \text{ m})\sqrt{\frac{9.5 \text{ N/m}}{0.250 \text{ kg}}} = \boxed{0.28 \text{ m/s}}$$

- (c) When the cart is 14 cm from the left end of the track, it has a displacement of $x = 14 \text{ cm} - 12 \text{ cm} = 2.0 \text{ cm}$ from the equilibrium position. The speed of the cart at this distance from equilibrium is

$$v = \sqrt{\frac{k}{m}(A^2 - x^2)} = \sqrt{\frac{9.5 \text{ N/m}}{0.250 \text{ kg}}[(0.045 \text{ m})^2 - (0.020 \text{ m})^2]} = \boxed{0.25 \text{ m/s}}$$

- 13.31** The period of a simple pendulum is $T = 2\pi\sqrt{L/g}$ where L is its length. The number of complete oscillations per second (that is, the frequency) for this pendulum is then given by

$$f = \frac{1}{T} = \frac{1}{2\pi} \sqrt{\frac{g}{L}} = \frac{1}{2\pi} \sqrt{\frac{9.80 \text{ m/s}^2}{2.00 \text{ m}}} = 0.352 \text{ s}^{-1}$$

Hence, the number of oscillations in a time $\Delta t = 5.00 \text{ min} = 300 \text{ s}$ is

$$N = f(\Delta t) = (0.352 \text{ s}^{-1})(300 \text{ s}) = 105.7 \text{ or } \boxed{105 \text{ complete oscillations}}$$

- 13.37** (a) The amplitude, A , is the maximum displacement from equilibrium. Thus, from Figure P13.37, $A = \frac{1}{2}(18.0 \text{ cm}) = \boxed{9.00 \text{ cm}}$

(b) The wavelength, λ , is the distance between successive crests (or successive troughs). From Figure P13.37, $\lambda = 2(10.0 \text{ cm}) = \boxed{20.0 \text{ cm}}$

(c) The period is $T = \frac{1}{f} = \frac{1}{25.0 \text{ Hz}} = 4.00 \times 10^{-2} \text{ s} = \boxed{40.0 \text{ ms}}$

(d) The speed of the wave is $v = \lambda f = (0.200 \text{ m})(25.0 \text{ Hz}) = \boxed{5.00 \text{ m/s}}$

- 13.39** (a) $T = \frac{1}{f} = \frac{1}{88.0 \times 10^6 \text{ Hz}} = 1.14 \times 10^{-8} \text{ s} = \boxed{11.4 \text{ ns}}$

(b) $\lambda = \frac{v}{f} = \frac{3.00 \times 10^8 \text{ m/s}}{88.0 \times 10^6 \text{ Hz}} = \boxed{3.41 \text{ m}}$

- 13.43** The down and back distance is $4.00 \text{ m} + 4.00 \text{ m} = 8.00 \text{ m}$.

The speed is then $v = \frac{d_{\text{total}}}{t} = \frac{4(8.00 \text{ m})}{0.800 \text{ s}} = 40.0 \text{ m/s} = \sqrt{F/\mu}$

Now, $\mu = \frac{m}{L} = \frac{0.200 \text{ kg}}{4.00 \text{ m}} = 5.00 \times 10^{-2} \text{ kg/m}$, so

$$F = \mu v^2 = (5.00 \times 10^{-2} \text{ kg/m})(40.0 \text{ m/s})^2 = \boxed{80.0 \text{ N}}$$

- 13.49 (a) The tension in the string is $F = mg = (3.0 \text{ kg})(9.80 \text{ m/s}^2) = 29 \text{ N}$. Then, from $v = \sqrt{F/\mu}$, the mass per unit length is

$$\mu = \frac{F}{v^2} = \frac{29 \text{ N}}{(24 \text{ m/s})^2} = \boxed{0.051 \text{ kg/m}}$$

- (b) When $m = 2.00 \text{ kg}$, the tension is

$$F = mg = (2.0 \text{ kg})(9.80 \text{ m/s}^2) = 20 \text{ N}$$

and the speed of transverse waves in the string is

$$v = \sqrt{\frac{F}{\mu}} = \sqrt{\frac{20 \text{ N}}{0.051 \text{ kg/m}}} = \boxed{20 \text{ m/s}}$$

- 13.52 (a) If the end is fixed, there is inversion of the pulse upon reflection. Thus, when they meet, they cancel and the amplitude is $\boxed{\text{zero}}$.
- (b) If the end is free there is no inversion on reflection. When they meet the amplitude is $A' = 2A = 2(0.15 \text{ m}) = \boxed{0.30 \text{ m}}$.