

Lorentz Transformation:

$$x' = \gamma(x - vt)$$

$$y' = y$$

$$z' = z$$

$$t' = \gamma(t - vx/c^2)$$

Inverse Lorentz Transformation:

$$x = \gamma(x' + vt')$$

$$y = y'$$

$$z = z'$$

$$t = \gamma(t' + vx'/c^2)$$

Relativistic transformation of velocities

$$u'_x = (u_x - v) / (1 - u_x v / c^2)$$

$$u'_y = u_y / \gamma(1 - u_x v / c^2)$$

Inverse Transformation:

$$u_x = (u'_x + v) / (1 + u'_x v / c^2)$$

$$u_y = u'_y / \gamma(1 + u'_x v / c^2)$$

Relativistic Doppler Effect:

$$f_{obs} = \sqrt{\frac{1 + v/c}{1 - v/c}} f_{source} \text{ (approaching)}$$

Relativistic Momentum

$$p_x = \gamma m u_x \quad ; \text{ similarly for y- and z-components}$$

$$\gamma = \frac{1}{\sqrt{1 - u^2/c^2}}$$

$$\text{Kinetic Energy } K = \gamma m c^2 - m c^2$$

$$\text{Total Energy } E = \gamma m c^2 = K + m c^2$$

$$E^2 = p^2 c^2 + m^2 c^4$$

$$\text{Force due to Electric field : } \mathbf{F} = q\mathbf{E}$$

$$\text{Force due to Magnetic Field: } \mathbf{F} = q\mathbf{v} \times \mathbf{B}$$

Particle of charge q moving in magnetic field \mathbf{B} in circle of radius r has relativistic momentum $p = qBr$

Stefan's Law $e_r = \sigma T^4$ $\sigma = 5.67 \cdot 10^{-8} \text{ Wm}^{-2}\text{K}^{-4}$

Planck's Blackbody radiation formula: $u(f, T)df = \frac{8\pi hf^3}{c^3} \left(\frac{1}{e^{hf/kT} - 1} \right) df$

De Broglie wavelength $\lambda = h/p$

Energy of photon $E = hf$

For photon $\lambda f = c$

Compton formula $\lambda' - \lambda = (h/m_e c)(1 - \cos \varphi)$

Bragg's Law $n\lambda = 2d \sin \theta$ ($n=1, 2, \dots$)

Drag Force on drop of radius α and velocity v in medium of viscosity η (always opposite to direction of v): $D = 6\pi\alpha\eta v = C v$

Rutherford's formula for scattering of alpha particles from nucleus of charge Z :

$$\Delta n = \frac{k^2 Z^2 e^4 N n A}{4 R^2 \left(\frac{1}{2} m_\alpha v_\alpha^2 \right)^2 \sin^4(\phi/2)}$$

Bohr's quantization for Angular momentum $mvr = n\hbar$

Energy levels of Bohr atom

$$E_n = -\frac{ke^2}{2a_0} \left(\frac{1}{n^2} \right) = -\frac{13.6}{n^2} \text{ eV}$$

$$\text{Bohr Radius } a_0 = \frac{\hbar^2}{me^2 k} = 0.5292 \cdot 10^{-10} \text{ m}$$

$$\text{Rydberg Constant } R = \frac{ke^2}{2a_0 hc} = 1.097 \cdot 10^7 \text{ m}^{-1}$$

$$\text{linear momentum operator } p_x = -i\hbar \frac{\partial}{\partial x}$$

$$\text{Angular momentum operator about z-axis } L_z = -i\hbar \frac{\partial}{\partial \phi}$$

Heisenberg Uncertainty principles: $\Delta p_x \Delta x \geq \hbar / 2$
 $\Delta E \Delta t \geq \hbar / 2$

$$\text{One-dimensional time-independent Schrodinger Equation } -\frac{\hbar^2}{2m} \frac{d^2\psi}{dx^2} + U(x)\psi = E\psi$$

$$\text{3-dimensional time-independent Schrodinger Equation } -\frac{\hbar^2}{2m} \nabla^2 \psi + U\psi = E\psi$$

$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} = \frac{\partial^2}{\partial r^2} + \left(\frac{2}{r}\right) \frac{\partial}{\partial r} + \frac{1}{r^2} \left[\frac{\partial^2}{\partial \theta^2} + \cot \theta \frac{\partial}{\partial \theta} + \csc^2 \theta \frac{\partial^2}{\partial \phi^2} \right]$$

The expectation value of some function of x, f(x) is given by $\int_{-\infty}^{\infty} dx P(x) f(x)$ where

P(x)dx is the (normalized) probability distribution for getting a value of x between x and x + dx.

Expectation value of some quantum mechanical operator O:

$$\langle O \rangle = \int_{-\infty}^{\infty} dx \psi^*(x) O \psi(x)$$

Relation between eigenfunctions, operators, and eigenvalues:

$$O \psi_n(x) = o_n \psi_n(x)$$

Standard deviation error for a variable represented by operator O:

$$\Delta O = \sqrt{\langle O^2 \rangle - \langle O \rangle^2}$$

Electron current through unit area for free electrons = $v |A|^2$; v = velocity of electrons; A = amplitude of plane wave.

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\text{proton mass} = 1.675 \cdot 10^{-27} \text{ kg} = 939.6 \text{ MeV}/c^2$$

electron mass

$$m_e = 9.1 \times 10^{-31} \text{ Kg} = 0.511 \text{ MeV} / c^2$$

$$c = 3 \times 10^8 \text{ m} / \text{s}$$

$$1 \text{ MeV} = 1.6 \times 10^{-13} \text{ J}$$

$$1 \text{ MeV} / c^2 = 1.78 \times 10^{-30} \text{ Kg}$$

$$1 \text{ MeV} / c = 5.344 \times 10^{-22} \text{ Kg.m} / \text{s}$$

$$1 \text{ eV} = 1.6 \cdot 10^{-19} \text{ J}$$

$$h = 6.626 \cdot 10^{-34} \text{ J.s} = 4.136 \cdot 10^{-15} \text{ eV.s}$$

$$\hbar = h / 2\pi = 1.055 \cdot 10^{-34} \text{ J.s} = 6.582 \cdot 10^{-16} \text{ eV.s}$$

$$\text{Coulomb's constant } k = 1 / (4\pi\epsilon_0) = 8.99 \cdot 10^9 \text{ N.m}^2 / \text{kg}^2$$

$$\text{Bohr radius } a_0 = 0.529 \cdot 10^{-10} \text{ m}$$

$$1 \text{ Rydberg (Energy required to ionize hydrogen atom)} = 13.6 \text{ eV}$$

Rydberg Constant $R = 1.097 \cdot 10^7 \text{ m}^{-1}$