

8.1 Photons

Photon energies - Interactions of light with matter.

- Ionizing radiation
- Radiation damage
- x-rays
- Compton effect
- X-ray diffraction

Photon Energy

Find the energy of a photon with a wavelength of 500 nm. Use units of electron volts ($1\text{eV} = 1.60 \times 10^{-19}\text{ J}$)

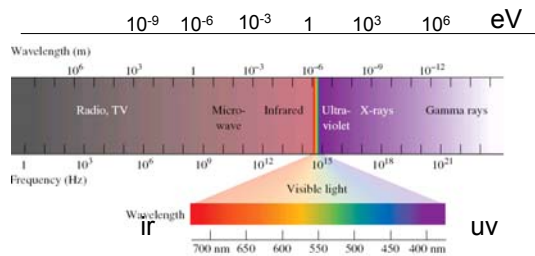
$$E = hf = h \frac{c}{\lambda} = 6.63 \times 10^{-34} \text{ Js} \left(\frac{3 \times 10^8 \text{ m/s}}{500 \times 10^{-9} \text{ m}} \right) = 4.0 \times 10^{-19} \text{ J}$$

$$E = \frac{4 \times 10^{-19} \text{ J}}{1.6 \times 10^{-19} \text{ J/eV}} = 2.5 \text{ eV}$$

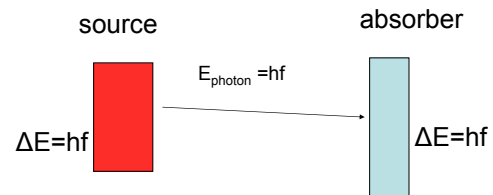
An electron volt is the energy change in moving an electron across a potential of 1 volt. A few electron volts is the energy of electrons in molecules. This is why visible light is absorbed by molecules (pigment molecules).

Photon Energies (eV)

$$E = hf = hc/\lambda$$



Photon concept



Light energy is has specific energies i.e. is quantized in the interaction of light with matter. Photons of different wavelengths, interact with different molecular properties- either in the generation of the photon or the absorption of the photon.

Photons

light	Typical Wavelength (m)	Typical Photon energy (eV)	Molecular interactions	applications
radio	10	10^{-7} eV	nuclear magnetic	NMR imaging
microwaves	10^{-2}	10^{-4} eV	Molecular rotations	Microwave oven cell phone
Infrared	10^{-5}	10^{-1} eV	Molecular vibrations	Heat lamp
Visible	400-700 nm	2-3 eV	Low energy electrons (pigments)	Vision Photosynthesis Photography
Ultraviolet	200-300 nm	4-5 eV	bonding electrons	Radiation damage Skin cancer
X-rays	1 nm	10^4 eV	Electrons scattering, tightly bound electrons	X-ray imaging X-ray diffraction

Microwave Oven

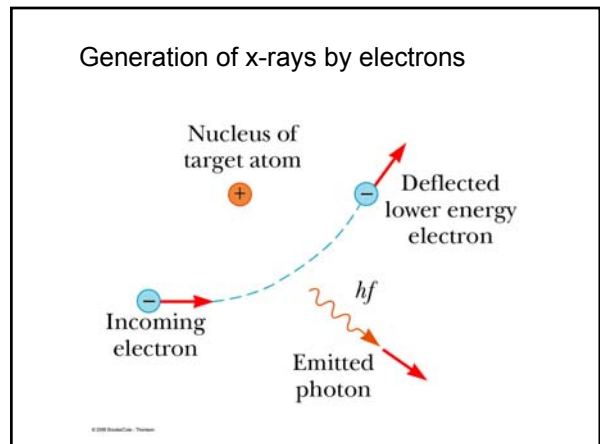
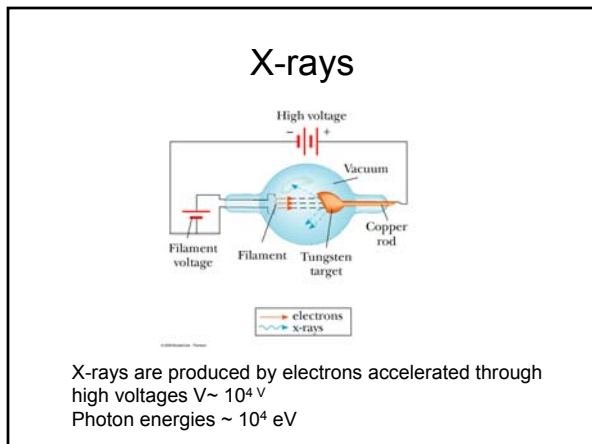
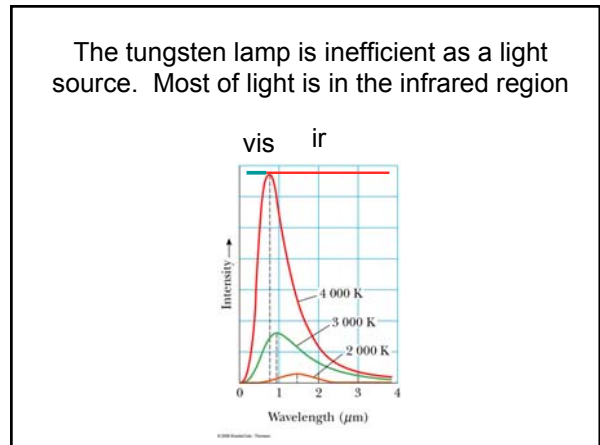
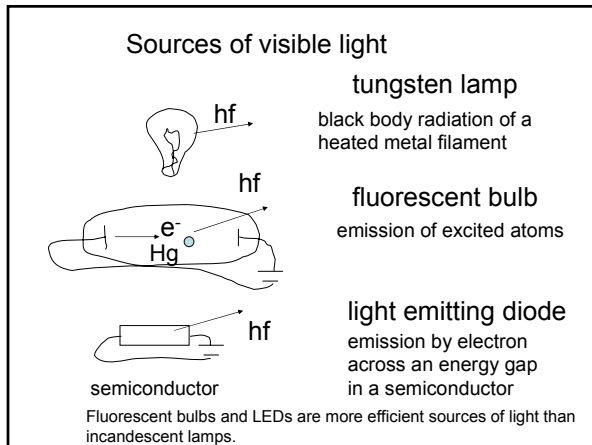
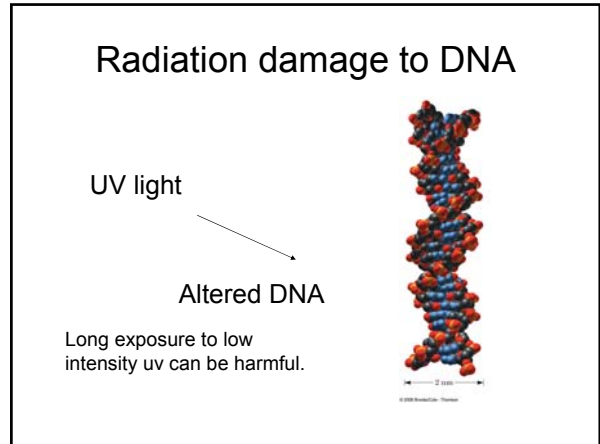
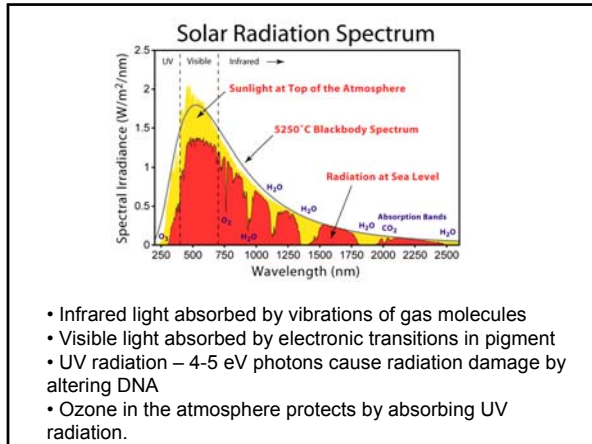
$$f = 10\text{GHz}$$

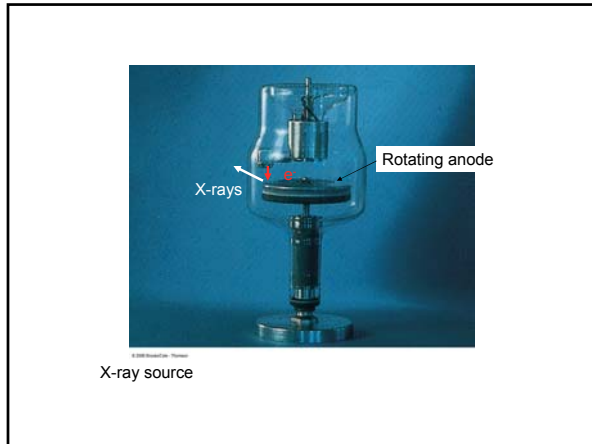
$$hf = 4 \times 10^{-5} \text{ eV}$$



Heats by exciting molecular rotations and vibrations.

Cell phones use the same frequency range but at much lower intensity.





X-rays

A Quantum Effect.
The maximum photon energy is ~ equal to the kinetic energy of the electron.

$$e\Delta V = hf_{\max} = \frac{hc}{\lambda_{\min}}$$

X-ray spectrum produced by 35 keV electrons hitting a molybdenum target.

Question

Find the minimum x-ray wavelength for a 35 keV electron.

$hf = KE$
(neglect work function - it is small compared to x-ray energies)

$KE = 35 \times 10^3 \text{ eV} \times (1.6 \times 10^{-19} \text{ J/eV}) = 5.6 \times 10^{-15} \text{ J}$

$E = hf = \frac{hc}{\lambda} = KE$

$\lambda = \frac{hc}{KE} = \frac{6.63 \times 10^{-34} \text{ Js} (3.0 \times 10^8 \text{ m/s})}{5.6 \times 10^{-15} \text{ J}} = 3.6 \times 10^{-11} \text{ m}$
0.036 nm

x-ray imaging

x-ray photograph of Wolfgang Roentgen's wife's hand.

x-rays penetrate soft tissue (light atoms) but are absorbed by heavy metal atoms. eg. Calcium, Gold

Compton scattering of x-rays.
High energy photons knock electrons out light atoms such as carbon.

The wavelength of a photon scattered from an electron is shifted to **longer wavelengths** due to loss of photon energy.

$$\Delta\lambda = \lambda - \lambda_0 = \frac{h}{m_e c} (1 - \cos\theta)$$

The Compton effect shows the particle nature of light.

X-ray diffraction

- X-rays have wavelengths close to atomic dimensions
- Crystalline solids have an ordered array of atoms that scatter x-rays much like a three-dimensional diffraction grating
- The x-ray diffraction pattern from crystals of molecules can be used to determine the density of scattering electrons (i.e. the electron density) and thus the molecular structure.

