

# Physics 222 UCSD/225b UCSB

## Lecture 1

- Reminder:
  - Bjorken Scaling
- QCD and Scaling violations
- Reminder:
  - PDF
  - Parton-Parton luminosities
- Outlook on this Quarter

# Logic of what we did:

- Electron - muon scattering in lab frame
  - Show what spin 1/2 on spin 1/2 scattering looks like for point particles.
- Elastic electron - proton scattering
  - Introduce the concept of form factors
  - Show how the charge radius of proton is determined
- Inelastic electron - proton scattering
  - Parameterize cross section instead of amplitude
- Deep inelastic electron - proton scattering
  - Discuss Bjorken scaling
  - Introduce partons and parton density function
  - Discuss parton density function of proton
- Construct “parton-parton luminosity” for pp and ppbar
  - Explain the excitement about the LHC

# Cross section for inelastic electron proton scattering

$$\left. \frac{d\sigma}{d\Omega} \right|_{lab} = \frac{4\alpha^2}{4E^2 \sin^4 \frac{\theta}{2}} \left[ W_2 \cos^2 \frac{\theta}{2} + 2W_1 \sin^2 \frac{\theta}{2} \right]$$

$$W_i = W_i(\nu, q^2)$$

$p$  = incoming proton 4-momentum

$k$  = incoming electron 4-momentum

$k'$  = outgoing electron 4-momentum

$m$  = proton mass

$$q^2 = (k - k')^\mu (k - k')_\mu$$

$$\nu \equiv \frac{p \cdot q}{m}$$

See H&M chapter 8.3 for details.

# Deep inelastic scattering

- Intuitively, it seems obvious that small wavelength, i.e. large  $-q^2$ , virtual photons ought to be able to probe the charge distribution inside the proton.
- If there are pointlike spin 1/2 particles, i.e. “quarks” inside, then we ought to be able to measure their charge via electron-proton scattering at large  $-q^2$ .
- *Within the formalism so far, this means that we measure  $W_1$  and  $W_2$  to have a form that indicates pointlike spin 1/2 particles.*

***What's that form?***

***Let's compare e-mu, and deep inelastic scattering.***

**Electron muon:**

$$\left. \frac{d\sigma}{dE'd\Omega} \right|_{lab} = \frac{4\alpha^2 E'^2}{q^4} \left[ \cos^2 \frac{\theta}{2} - \frac{q^2}{2m^2} \sin^2 \frac{\theta}{2} \right] \delta \left( v + \frac{q^2}{2m} \right)$$

**Inelastic electron proton:**

$$\left. \frac{d\sigma}{dE'd\Omega} \right|_{lab} = \frac{4\alpha^2 E'^2}{q^4} \left[ W_2 \cos^2 \frac{\theta}{2} + 2W_1 \sin^2 \frac{\theta}{2} \right]$$

**From this we concluded that  $W_1$  and  $W_2$  for a point particle are given by:**

$$W_1 = -(q^2/2M^2) \delta[v + (q^2/2m)]$$

$$W_2 = \delta[v + (q^2/2m)]$$

# Rewriting and simplifying:

- Let's replace  $-q^2$  by  $Q^2$  in order to always have a positive  $Q^2$  value in all our expressions.
- Mathematical aside:  $\delta[ax] = \delta[x]/a$
- Notational aside:  $x = \frac{Q^2}{2p \cdot q} = \frac{Q^2}{2m\nu}$

*x is a dimensionless quantity that is interpreted as the longitudinal momentum fraction of the parton inside the proton.*

# $W_1, W_2$ for point particles in proton

$$2mW_1 = \frac{Q^2}{2m} \delta\left(v - \frac{Q^2}{2m}\right) \Rightarrow 2mW_1 = \frac{Q^2}{2m\nu} \delta\left(1 - \frac{Q^2}{2m\nu}\right)$$

$$\nu W_2 = \delta\left(1 - \frac{Q^2}{2m\nu}\right)$$

Both of these structure functions are now functions of only one dimensionless variable,  $x$  !!!

**$\Rightarrow$  Bjorken Scaling**

Both of these structure functions are obviously related. In this case, there is only one  $F(x)$ .

# Scaling as characteristic of point particles inside the proton

- To understand why the scale independence itself is the important characteristics of having point particles inside the proton, compare  $W_i$  for e-mu with elastic e-proton:

$$2mW_1 = \frac{Q^2}{2m\nu} \delta\left(1 - \frac{Q^2}{2m\nu}\right) \quad 2MW_1^{elastic} = G(Q^2) \frac{Q^2}{2M\nu} \delta\left(1 - \frac{Q^2}{2M\nu}\right)$$

$$\nu W_2 = \delta\left(1 - \frac{Q^2}{2m\nu}\right) \quad \nu W_2^{elastic} = G(Q^2) \delta\left(1 - \frac{Q^2}{2M\nu}\right)$$

- For elastic scattering, there is an explicit  $Q^2$  dependence. The 0.71GeV mass scale in the pole of  $G$  sets a size cut-off below which the proton is more likely to disintegrate than scatter elastically.

$$G = \frac{1}{\left(1 + \frac{Q^2}{0.71}\right)^2}$$



# Bjorken Scaling

$$\omega = \frac{2q \cdot p}{Q^2}$$

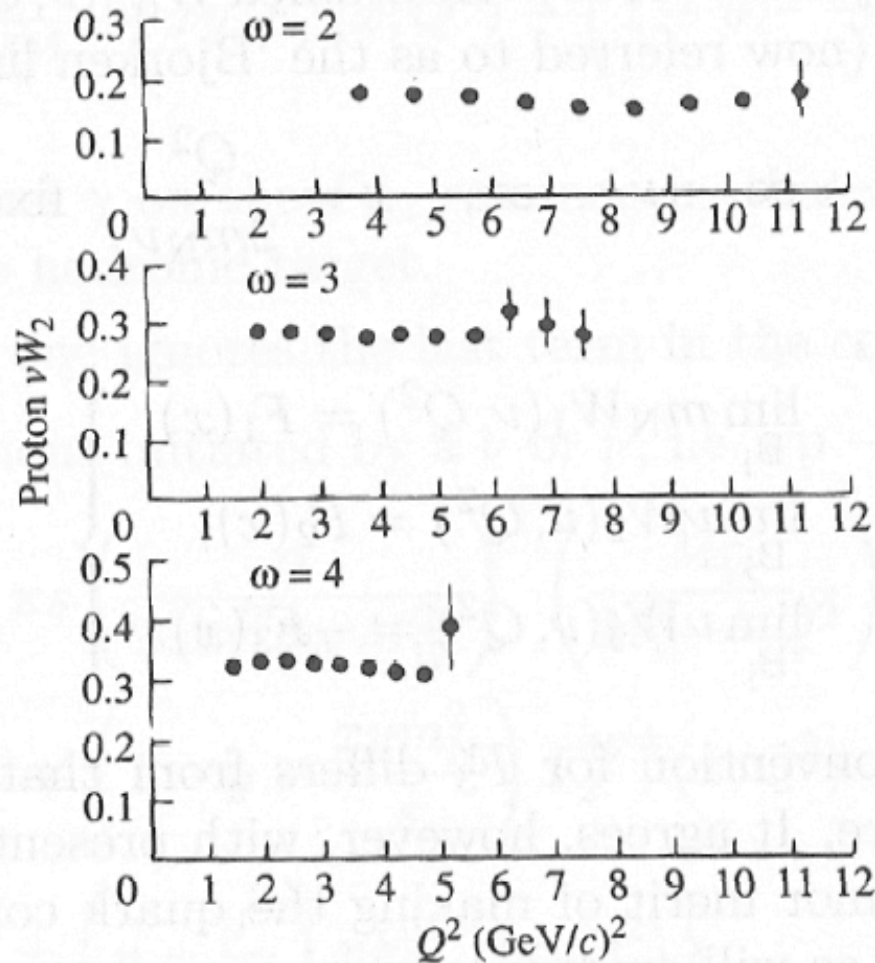
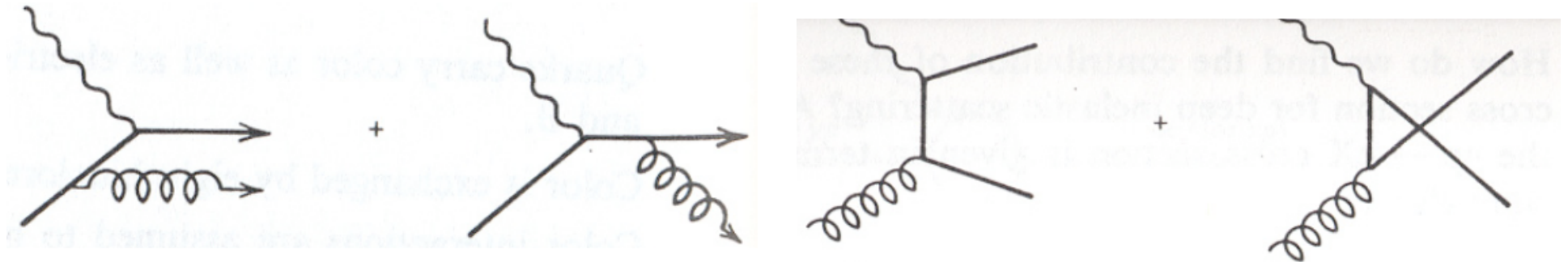


Fig. 15.9. Scaling behaviour of electromagnetic structure function  $\nu W_2$  at various  $\omega$  values. There is virtually no variation with  $Q^2$ . (From Panofsky, 1968.)

# Recap so far

- We saw that point particles inside the proton lead to Bjorken scaling
  - Historically this was essential to convince humanity that quarks exist in nature, and aren't just some group theory tool to explain spectroscopy.
- However, the proton isn't just non-interacting point particles with empty space in between.
  - We will now discuss the impact of QCD on the parton model “qualitatively”
  - See H&M chapter 10 for a more quantitative discussion.

# Lowest order QCD corrections to “naïve” Parton Model

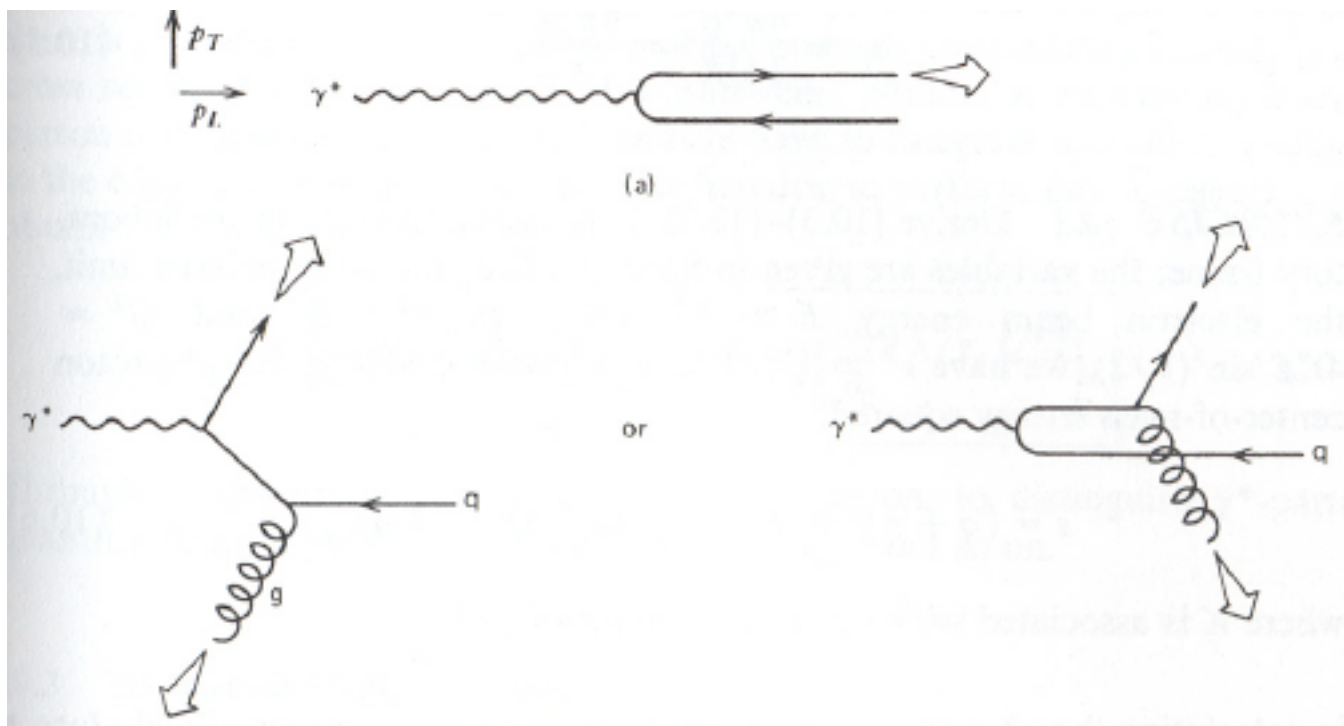


These diagrams have two experimentally visible consequences:

1. Outgoing quark no longer collinear with virtual photon.  
Or for hadron colliders, **COM of “hard collision” no longer has zero  $p_T$ .**
2. Scaling violation of the proton structure function.

# PT boost at Tevatron and LHC

- The primary source of transverse momentum of DY, Higgs production via gg, diboson production, etc. etc. etc. is gluon radiation.

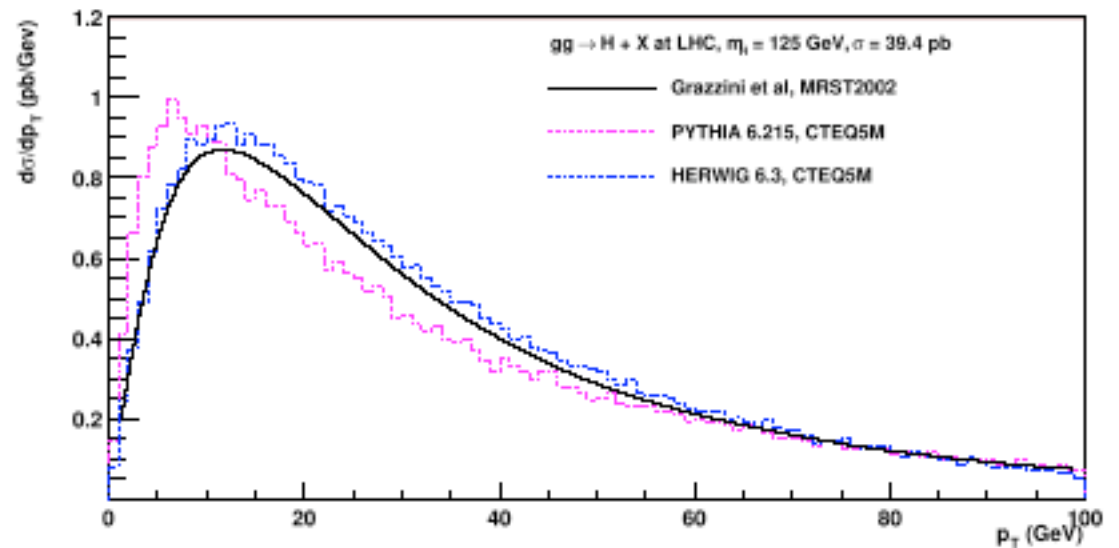
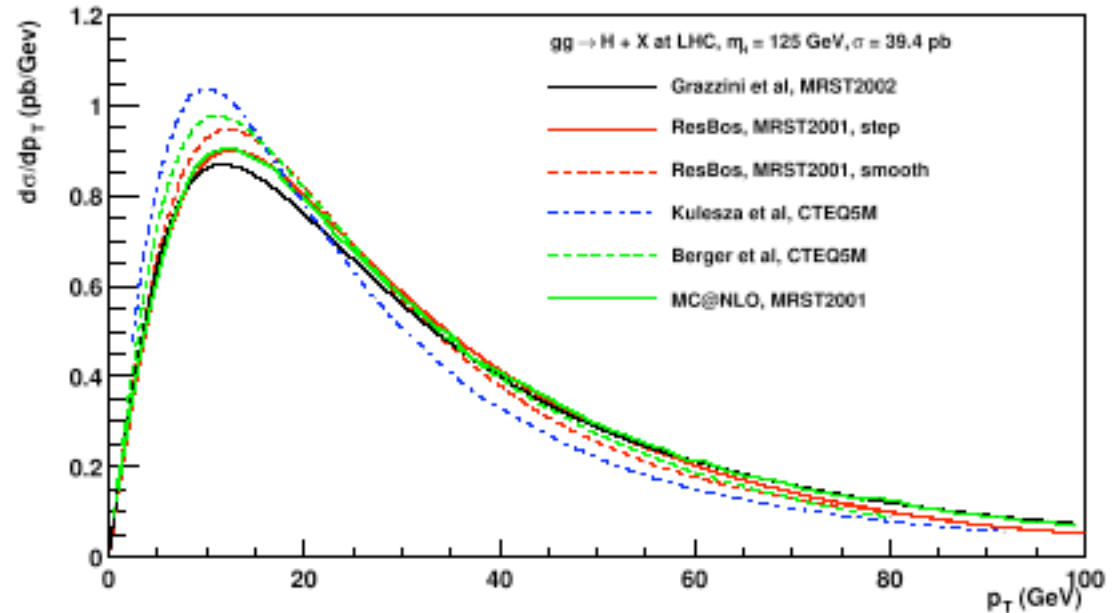


# Example: Higgs production

At “LO in QCD”,  $p_T = 0$  !!!

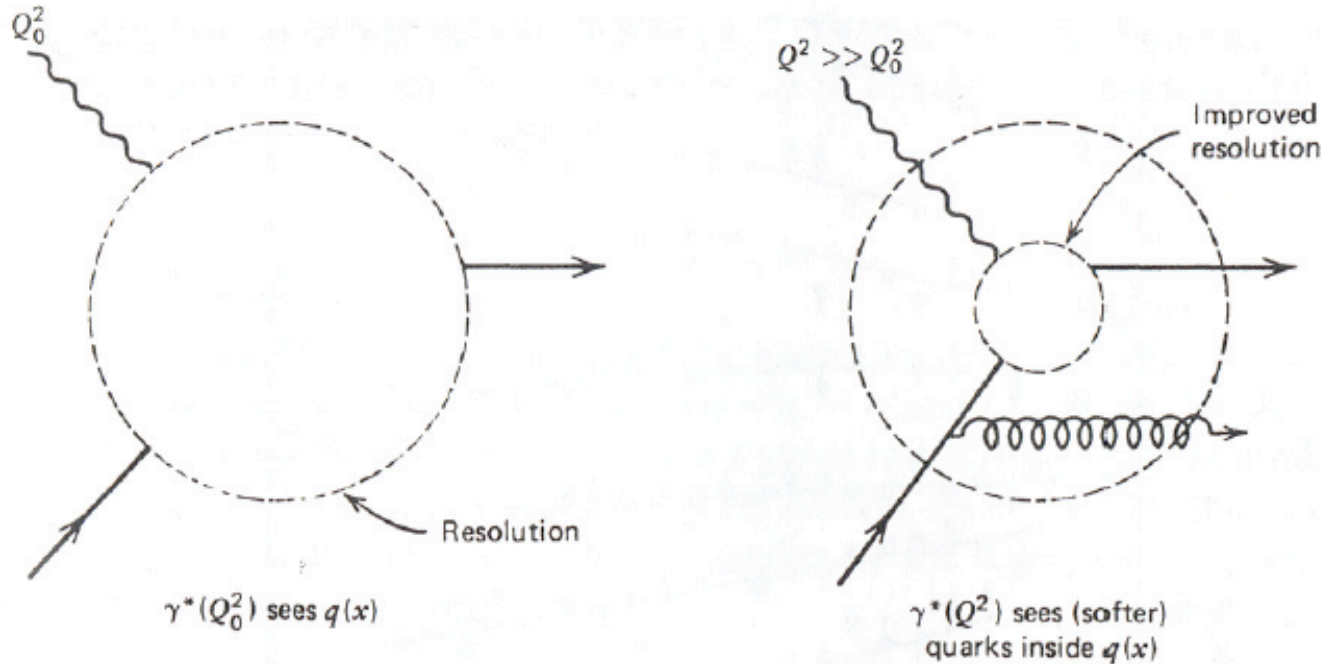
The differences are in the model used to “parameterize” higher order effects.

All distributions are normalized to the same area.



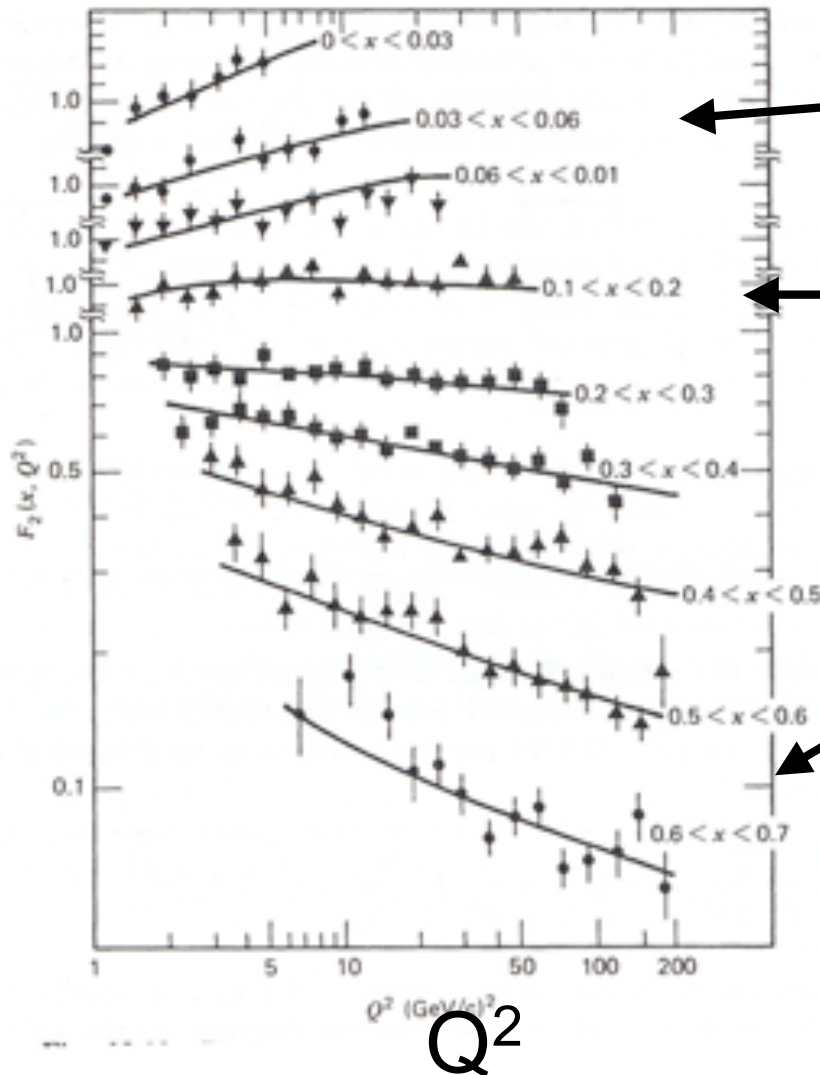
# Scaling Violation

- As  $Q^2$  increases, we probe shorter distances.



- At large  $Q^2$  the large  $x$  quarks are more likely to lose energy due to gluon radiation.
  - Increased quark content at low  $x$  and high  $Q^2$
  - Decreased quark content at large  $x$  and high  $Q^2$

# Resulting Structure Functions



Low x

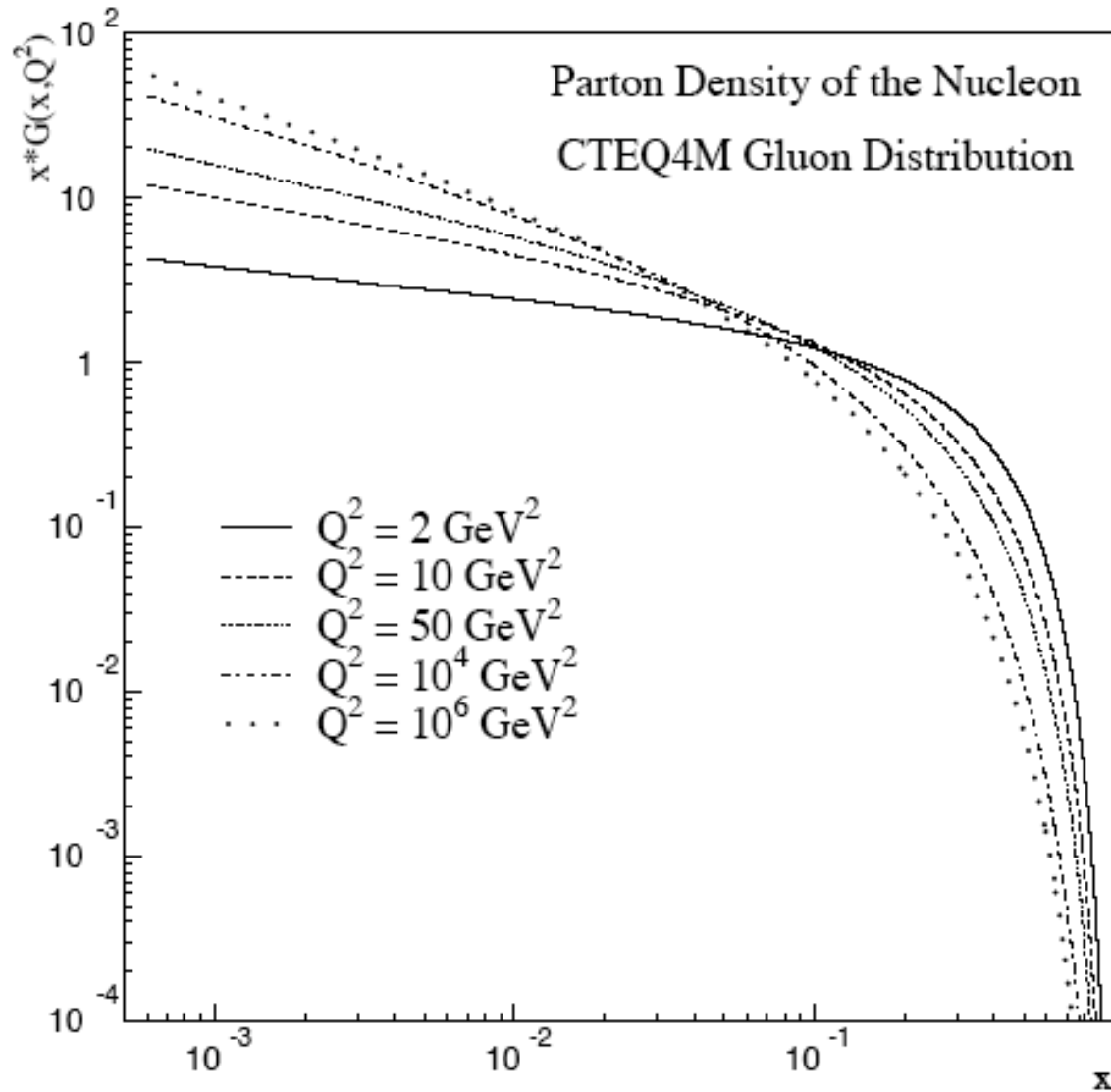
At low x: quark content increases with  $Q^2$

scaling at  $x \sim 0.1-0.2$

High x

At high x: quark content decreases with  $Q^2$

QCD predicts this behaviour.  
See discussion of  
Altarelli-Parisi equation  
in H&M chapter 10.



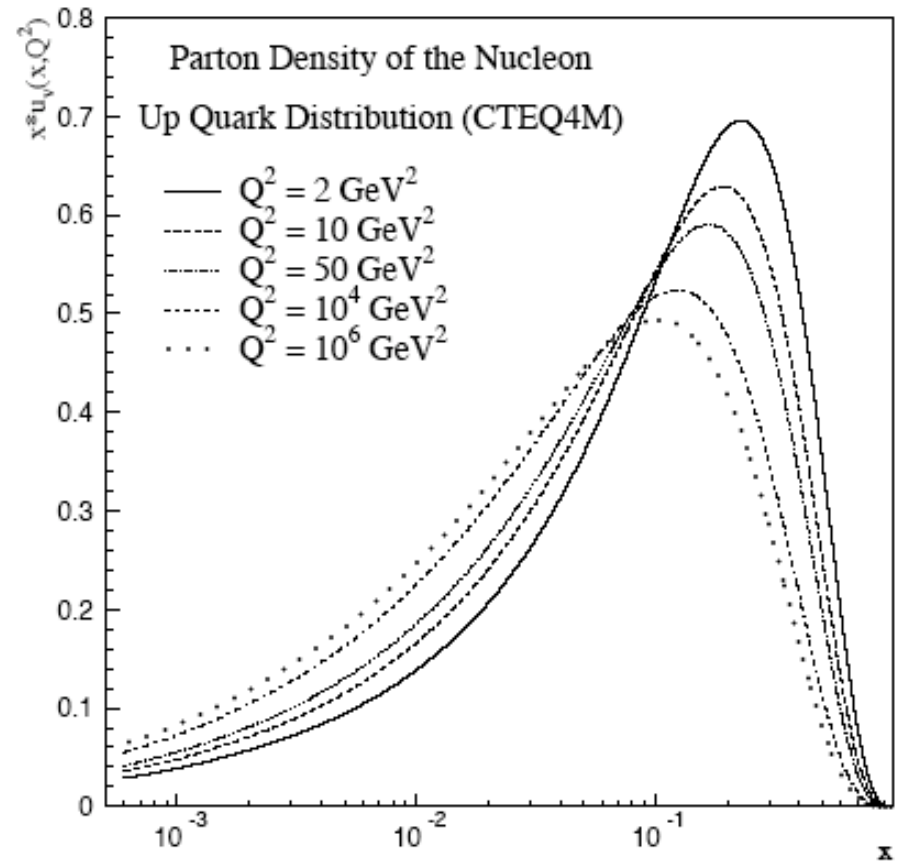
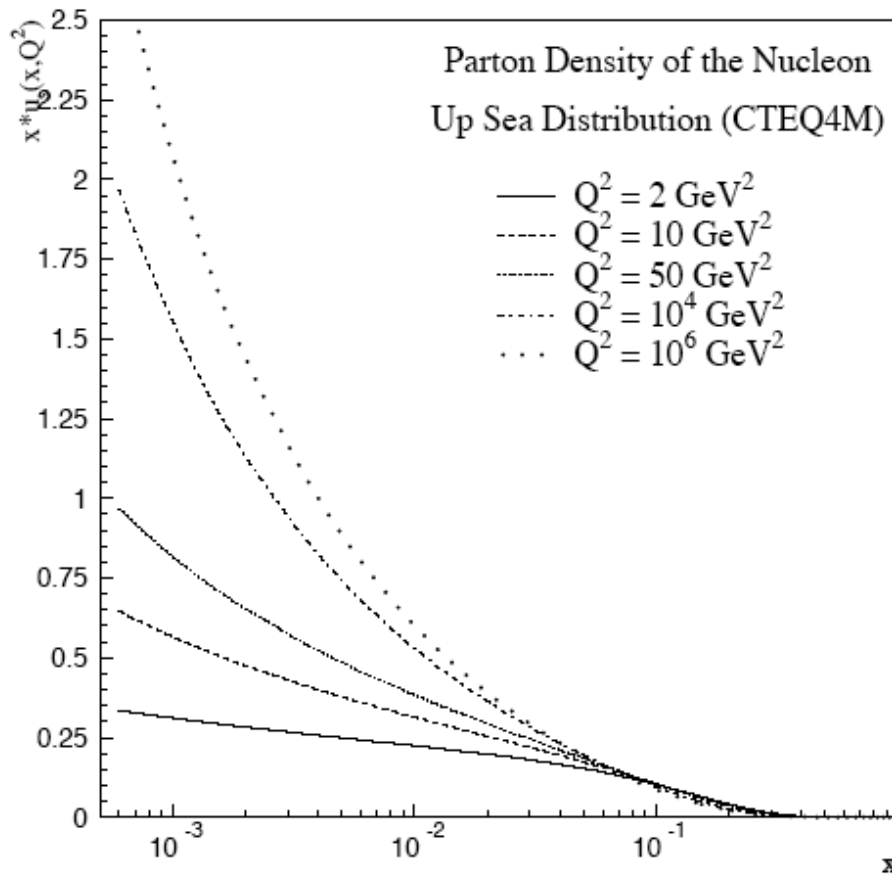
**Example:  
Gluon PDF**

(Axes are log scale!)

$Q^2$  dependence is moderate except for very small  $x$  and/or very small  $Q^2$ .



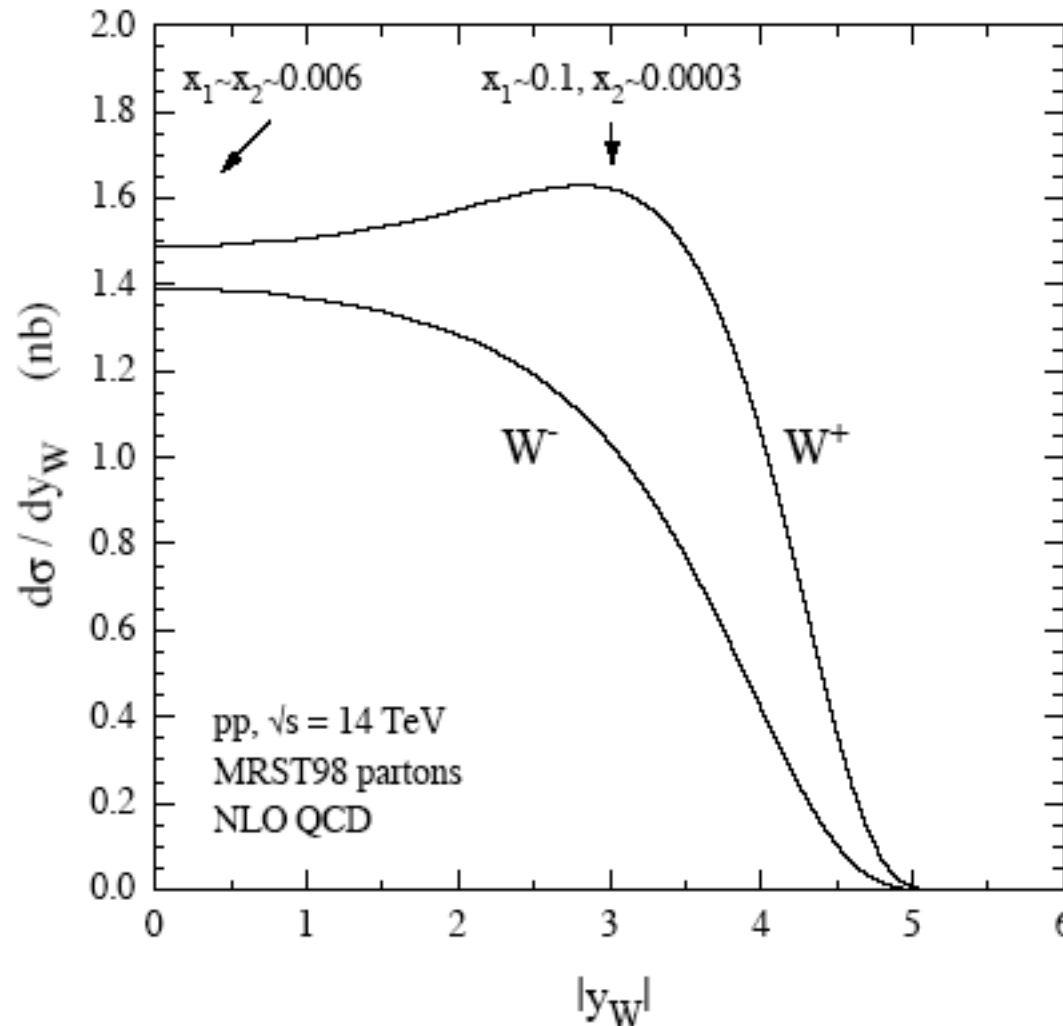
# Example: Up from valence & sea



Again, differences are large for small  $x$  and small  $Q^2$ .

(Y-axis is linear scale!)

# Aside: Predicted $W^+$ and $W^-$ cross section vs rapidity @ LHC



$u + d\bar{b} = W^+$

Proton = uud

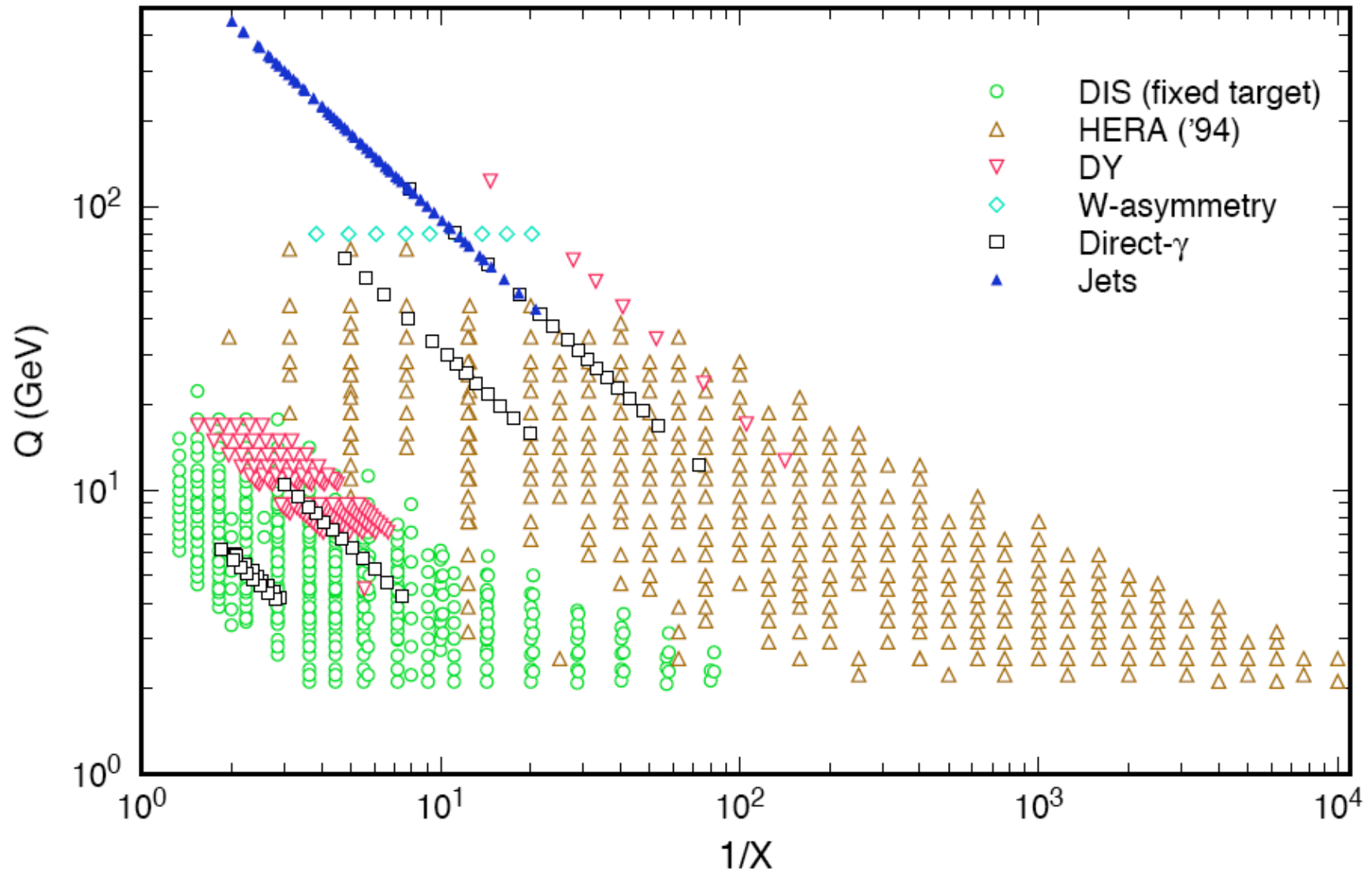
$\Rightarrow W^+$  production dominates at high rapidity, where valence quarks matter.

Recall:

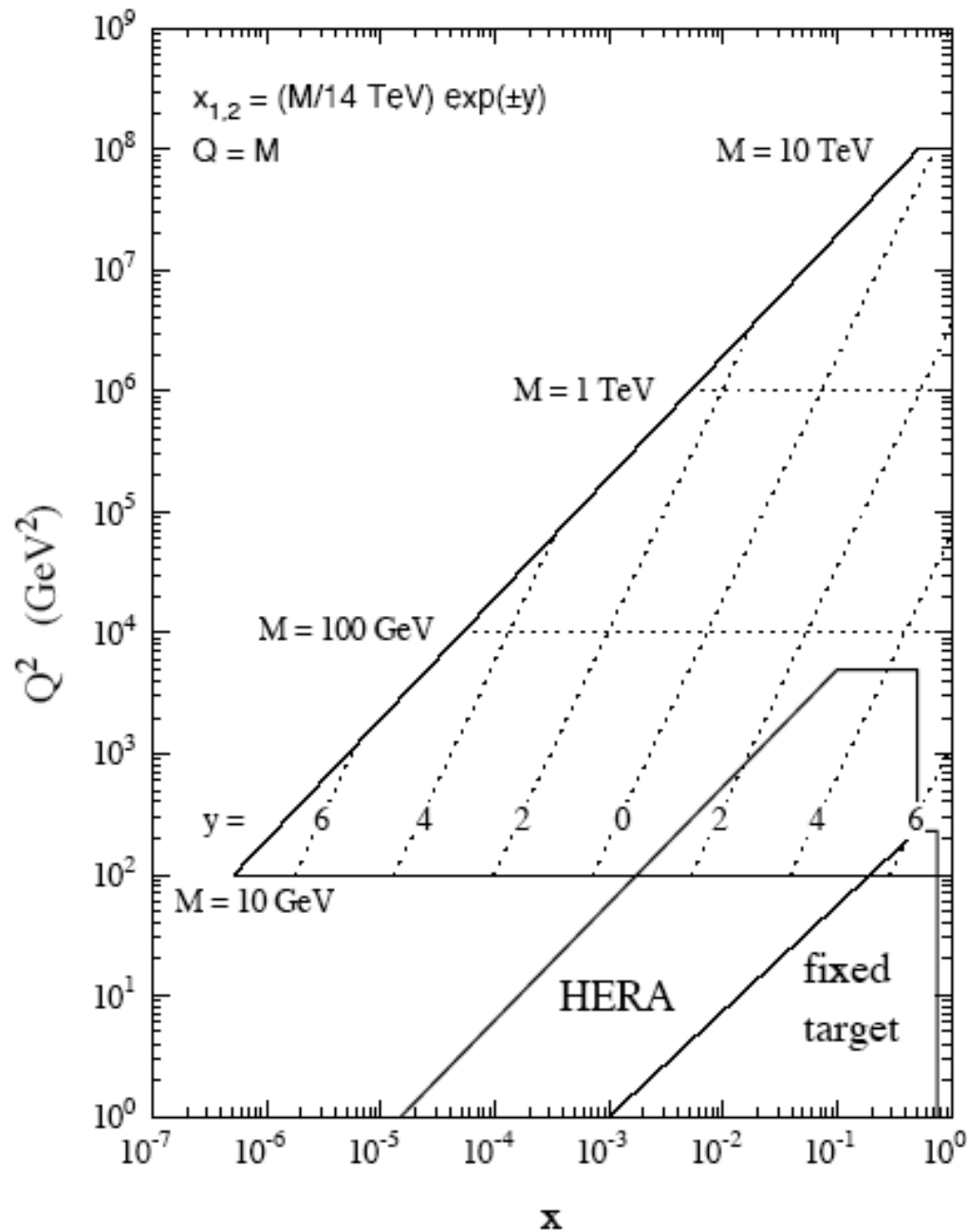
$$(m_W)^2 \sim x_1 x_2 S$$

While boost of  $W$  depends on imbalance of  $x_1, x_2$ .

# Sources of info on PDF's



## LHC parton kinematics

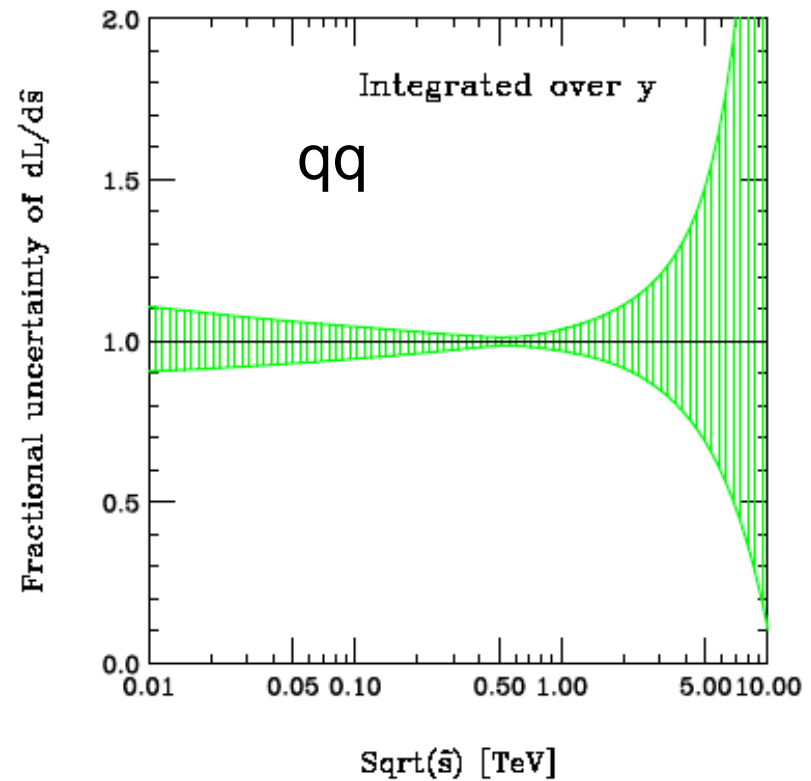
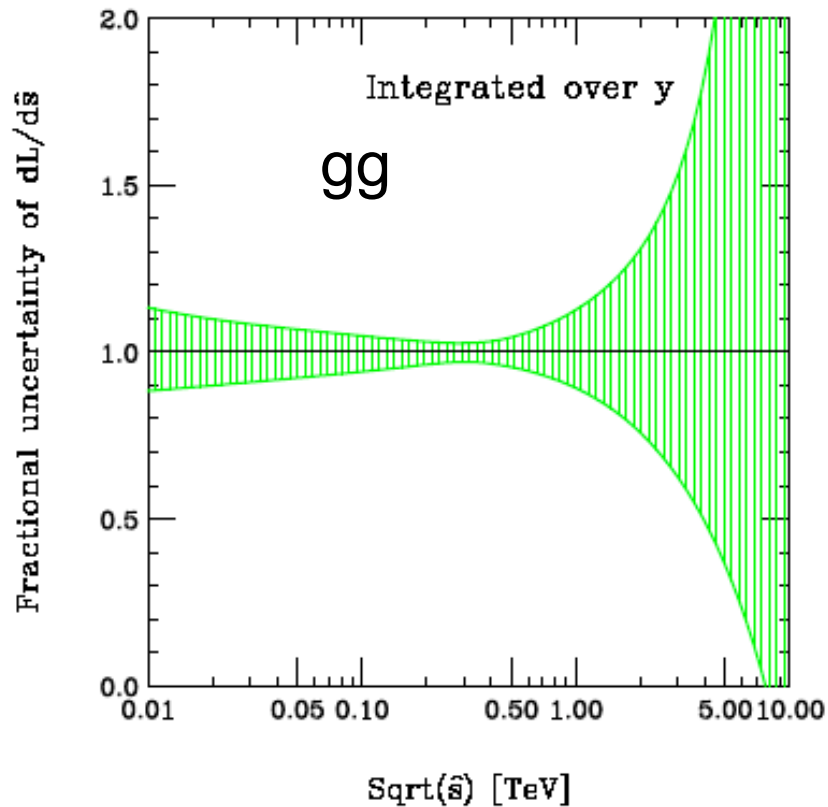


# LHC Parton Kinematics

*To accurately predict pdf's for the relevant kinematics, we depend on QCD evolution of the structure functions.*

So how well do we predict Parton-parton lumis at LHC?

# Uncertainty of parton-parton @ LHC



The larger  $x$  becomes, the larger the uncertainties.

# Topics we omitted

## and where to learn about them.

- Our treatment of QCD was by and large very simplistic.
  - More on QCD improved parton model
    - Chapter 10 of H&M.
  - More on QCD & collider physics, especially LHC.
    - <http://www.iop.org/EJ/abstract/0034-4885/70/1/R02/>
  - More on pdf's and what data they come from
    - Atlas paper by Joey Huston (see course website).
  - More on a large variety of topics in QCD and collider physics.
    - Ellis, Stirling, Webber: QCD and Collider Physics (see link on website)

# Outlook on this Quarter

- Chapter 12: Weak Interactions (3 lectures)
- Mixing and CP violation (3 lectures)
- Statistics (1 lecture)
- Chapter 13: Electroweak (1 lecture)
- Chapter 14: Gauge Symmetries & Spontaneous symmetry breaking (2 lectures)
- Chapter 15: Standard Model of EWK Interactions (1 lecture)
- SM Higgs hunting phenomenology (2 lectures)
- 2 Higgs Doublet Model (1 lecture)
- SUSY phenomenology (1 lecture)
- Your seminars (2 lectures)
- Total is 18 lectures, including today.
- There are two Mondays that are holidays: 1/18, 2/15.

