

Physics 2D Quiz 5 Solutions #1 p.1

e^- , accelerated through 8kV, non-relativistic

(a) What is the momentum?

Conservation of energy:

$$|qV| = \frac{1}{2}mv^2 = \frac{p^2}{2m} \Rightarrow p = \sqrt{2m|qV|}$$

$$p = \sqrt{2 \times 9.1 \times 10^{-31} \text{ kg} \left[-1.6 \times 10^{-19} \text{ C} \cdot 8000 \text{ V} \right]} = [4.83 \times 10^{-23} \text{ kg m/s}]$$

$$(b) \lambda = \frac{h}{p} = \frac{6.626 \times 10^{-34} \text{ Js}}{4.83 \times 10^{-23} \text{ kg m/s}} = [1.37 \times 10^{-11} \text{ m}]$$

#2 p.1

mysterious jungle where $\hbar = 50 \text{ Js}$

$\Delta x \approx 4 \text{ m}$, $m = 100 \text{ kg}$

(a) What is the minimum uncertainty in v ?

$\Delta x \Delta p \geq \hbar/2$, minimum uncertainty $\Rightarrow \Delta x \Delta p = \hbar/2$

$\Delta p = m \Delta v$ (we know the mass exactly).

$$\text{Therefore, we have } \Delta v = \frac{\hbar}{2m\Delta x} = \frac{\hbar}{4\pi m \Delta x}$$

$$\Delta v = \frac{50 \text{ Js}}{4\pi (100 \text{ kg})(4 \text{ m})} = [9.95 \times 10^{-3} \text{ m/s}]$$

$$(b) \Delta x = \Delta v t = (9.95 \times 10^{-3} \text{ m/s})(10 \text{ s}) = [9.95 \times 10^{-2} \text{ m}]$$