

PHYS 2D
PROBLEM SESSION

2012/4/26

2.12

- Solution for b is incorrect

Q: e^- with speed $0.75c$, find speed of proton with 1. same E_k , 2. same momentum

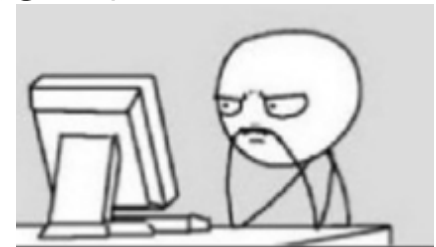
- e^- : $\gamma_e = 1.512$, $E_{ke} = (\gamma_e - 1)m_e c^2 = 0.262 \text{ MeV}$,
 $p_e = \gamma_e m_e v_e = 0.579 \text{ MeV}/c$

- proton:

- ◆ 1. $E_{kp} = (\gamma_p - 1)m_p c^2 = E_{ke} = 0.262 \text{ MeV}$,
 $\gamma_p = 0.262/931.5 + 1 = 1.000281$, $v_p = 0.0237c$

- ◆ 2. $p_p = \gamma'_p m_p v'_p = p_e = 0.579 \text{ MeV}/c$,
 $v'_p \gamma'_p = v'_p / (1 - (v'_p/c)^2)^{1/2} = c * 0.579 / 931.5 = a$
 $v'_p{}^2 = a^2 c^2 / (1 + a^2)$, $v'_p = 6.216 * 10^{-4} c$

- Solution just used γ_p from 1 for γ'_p (wrong)



3.14

Q: Shine 350nm light on potassium ($\phi=2.24\text{eV}$), find K_e & cutoff λ

- $E_{\text{photon}} = \phi + K_e$
- $E_{\text{photon}} = hc/\lambda = 6.626 \times 10^{-34} \times 3 \times 10^8 / (350 \times 10^{-9}) \text{J}$
 $= 5.68 \times 10^{-19} \text{J} = 3.55 \text{eV}$
- $K_e = 3.55 - 2.24 = 1.31 \text{eV}$
- Cutoff λ : E_{photon} is now a variable
- Cutoff happens at $K_e = 0$
- $E_{\text{photon}} = \phi = hc/\lambda = 2.24 \text{eV}$
- $\lambda = 555 \text{nm}$

3.14

- Solution has errors in formula

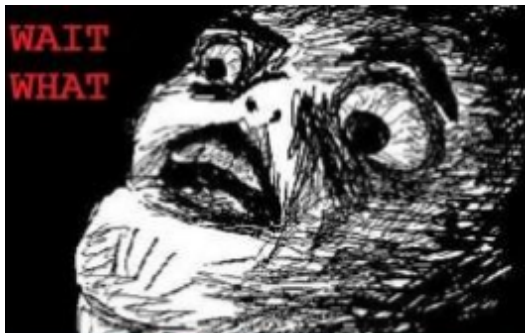
$$K = hf - \phi = \frac{hc}{\lambda - \phi}$$

$$\phi = \frac{hc}{\lambda - K}$$



$$K = hf - \phi = \frac{hc}{\lambda} - \phi$$

$$\phi = \frac{hc}{\lambda} - K$$



3.24

Q: 0.2nm X-ray scattered by e^- at 90° , find $\Delta\lambda$ & K_e

- Compton formula: $\lambda' - \lambda_0 = \frac{h}{m_e c} (1 - \cos\theta)$
- $\cos(90^\circ) = 0$
- $\Delta\lambda = h/m_e c = 0.00243\text{nm} > 0$
- $\lambda' > \lambda_0$
- $E_\lambda = E_{\lambda'} + K_e$
- $K_e = hc/\lambda_0 - hc/\lambda' = 1.19 \times 10^{-14}\text{J} = 74.6\text{eV}$

3.26

Q: 0.04nm X-ray scattered at θ , find λ' & K_e

□ $\lambda' - \lambda_0 = \frac{h}{m_e c} (1 - \cos \theta)$

□ $h/m_e c = 0.00243 \text{ nm}$

□ $K_e = hc/\lambda_0 - hc/\lambda'$

Q: Which θ produces largest K_e ?

□ 180°

□ Largest λ' , highest e^- momentum

3.26

More errors



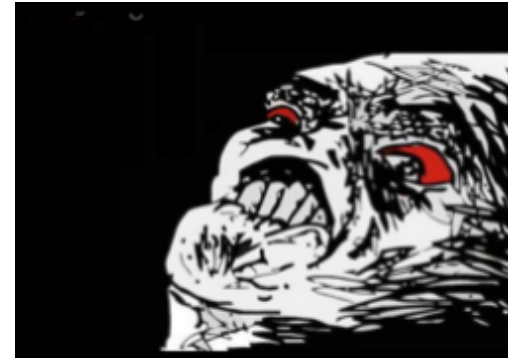
$$K_e hc \left(\frac{1}{\lambda_0} - \frac{1}{\lambda'} \right)$$

$$K_e = \frac{(6.63 \times 10^{-34} \text{ J s})(3 \times 10^8 \text{ m/s})}{\frac{1}{0.04 \times 10^{-9}} - \frac{1}{4.03 \times 10^{-11}}}$$



$$K_e = hc \left(\frac{1}{\lambda_0} - \frac{1}{\lambda'} \right)$$

$$K_e = (6.63 \times 10^{-34} \text{ J s})(3 \times 10^8 \text{ m/s}) \left(\frac{1}{0.04 \times 10^{-9}} - \frac{1}{4.03 \times 10^{-11}} \right)$$



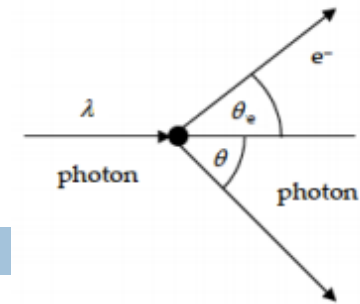
3.31

Q: 0.1 MeV photon Compton scattered at 60° , find

$E_{\lambda'}$, K_e & recoil angle of e^-

- $\Delta\lambda = h/mc(1 - \cos 60^\circ) = 0.00121 \text{ nm}$
- $\lambda = hc/E_\lambda = hc/0.1 \text{ MeV} = 0.0124 \text{ nm}$
- $\lambda' = 0.01361 \text{ nm}$
- $E_{\lambda'} = hc/\lambda' = 0.0911 \text{ MeV}$
- $K_e = E_\lambda - E_{\lambda'} = 8.89 \text{ KeV}$
- For the angle, need momentum conservation

3.31



- Momentum conservation in x (direction of incoming photon)

$$\text{photon: } E=pc=hc/\lambda, p=h/\lambda$$

$$p_{\text{before},x}=h/\lambda=p_{\text{after},x}=\cos 60^\circ h/\lambda'+\gamma m_e v \cos \theta_e$$

- Momentum conservation in y

$$p_{\text{before},y}=0=p_{\text{after},y}=-\sin 60^\circ h/\lambda'+\gamma m_e v \sin \theta_e$$

- $\gamma m_e v \sin \theta_e / \gamma m_e v \cos \theta_e$
 $=(\sin 60^\circ h/\lambda') / (h/\lambda - \cos 60^\circ h/\lambda')$

- $\tan \theta_e = 1.451, \theta_e = 55.4^\circ$

Example

- Calculate the binding energy in MeV per nucleon in the isotope carbon-12, $^{12}_6\text{C}$. The mass of a proton is 1.007276u and the mass of a neutron is 1.008665u where $1 \text{ u} = 929.494 \text{ MeV}/c^2$.

$$\Delta m = 6m_p + 6m_n - m_C = [6(1.007\,276) + 6(1.008\,665) - 12] \text{ u} = 0.095\,646 \text{ u}$$

$$\Delta E = (931.49 \text{ MeV/u})(0.095\,646 \text{ u}) = 89.09 \text{ MeV}$$

$$\text{Therefore the energy per nucleon} = \frac{89.09 \text{ MeV}}{12} = 7.42 \text{ MeV}$$

Formulas you might need

- $E=pc, E=hf=hc/\lambda$ (photon)
- $E^2 = (\mathbf{pc})^2 + (mc^2)^2$ (particle)
- $\sum_i \mathbf{E}_i^{\text{before}} = \sum_i \mathbf{E}_i^{\text{after}}, \quad \sum_i \mathbf{P}_i^{\text{before}} = \sum_i \mathbf{P}_i^{\text{after}}$ (note: p is a vector)
- $p=\gamma mu$
- $E=K+mc^2=\gamma mc^2$
- Compton: $\lambda' - \lambda_0 = \frac{h}{m_e c} (1 - \cos \theta)$
- Photoelectric: $E_{\text{photon}} = \phi + K_e$