

Show all steps in your calculations. Justify all answers. Write clearly.

Suggestion: do the problems you find easiest first

Some constants:

$$hc = 12,400eVA, \quad k_B = 1/11,600eV / K, \quad m_e c^2 = 511,000eV$$

$$\hbar c = 1973eVA \quad ; \quad ke^2 = 14.4eVA \quad ; \quad 1A = 10^{-10} m \quad ; \quad m_{neutron} c^2 = 939.6MeV$$

Problem 1 (10 pts)

10 million α particles with kinetic energy 7.2 MeV are incident on a tin foil ($Z=50$) of thickness 3μ (30,000A). Assume the density of tin is 0.333 atoms/A³.

- What is the distance of closest approach for a head-on collision with a tin nucleus, in A?
- What is the impact parameter (in A) for which α particles are scattered at a 90 degree angle?
- How many α particles are scattered at angles larger than 90 degrees, assuming the radius of the tin nucleus is smaller than the distance calculated in (a)?
- For extra credit (3 pts) Approximately how many α particles are scattered at angles between 90° and 92° ?

Problem 2 (10 pts)

According to classical electromagnetism, an electron moving in a circular orbit will emit electromagnetic radiation of frequency equal to its frequency of revolution, $f = v / 2\pi r$.

- Using formulas derived from the Bohr model of hydrogen, find an expression for the wavelength of the radiation that would be emitted by an electron in the n-th Bohr orbit according to classical electromagnetism.
- From your result in (a), find numerical values (in A) for those wavelengths for the orbits $n=4$ and $n=5$, λ_4 and λ_5 .
- Find the wavelength of the photon emitted or absorbed when an electron makes a transition between orbits $n=4$ and $n=5$ according to Bohr's theory. Give your answer for this wavelength, λ_{45} , in A.
- Compare λ_{45} with $(\lambda_4 + \lambda_5)/2$ and explain why they agree or disagree.

Problem 3 (10 pts)

An electron and a neutron have the same de Broglie wavelength. Find the ratio of the kinetic energy of the electron to the kinetic energy of the neutron:

- assuming they are both non-relativistic.
- assuming they are both extremely relativistic.
- Find the range of de Broglie wavelengths that a relativistic neutron will have.

Definitions:

non-relativistic: kinetic energy much smaller than rest energy

relativistic: kinetic energy equal or larger than rest energy

extremely relativistic: kinetic energy much much larger than rest energy