

Information (may or may not be needed):

At STP= 0°C , 1atm, ideal gas occupies 22.4L; 1atm= $1.013\times 10^5\text{Pa}$; $1\text{L}=10^{-3}\text{m}^3$;

$R=8.314\text{J}/(\text{K mol})=0.082\text{ L atm}/(\text{K mol})$; $1\text{u}=1.66\times 10^{-27}\text{kg}$; $k=1.38\times 10^{-23}\text{J/K}$

Avogadro's number: $N_A=6.02\times 10^{23}$

Problem 1 (10 pts)

On a given day, temperature is 0°C , pressure is 1atm, and relative humidity is 75%. The saturated vapor pressure of water at 0°C is $6.1\times 10^2\text{Pa}$. The molecular weight of water is 18. For the following questions, answers accurate to 1% are good. Assume all gases are ideal gases.

You put 10g of ice in a container that has volume 1.5L, put a lid on it that seals it, and wait a while.

- (a) Assuming air has molecular weight 29, how much air (in g) is there in the container?
- (b) What is the relative humidity in the air in the container?

Now you heat up the container and everything inside it to 100°C , and wait a while.

- (c) What is the total pressure inside the container, in atm?
- (d) How much liquid water (in g) is there in the container?

Problem 2 (10 pts (a, b, c) + 3 pts extra credit (d))

In an ideal gas with molecules of molecular weight 20u , the rms speed of the molecules is 600m/s .

- (a) What is the temperature, in K?

Hint: the average kinetic energy of a molecule is $(3/2)kT$.

- (b) If there are 1,000 molecules with speed between 600m/s and 605m/s , how many are there with speed between 1200m/s and 1210m/s ?
- (c) For every 1,000 molecules with velocity in the x direction v_x between 599m/s and 601m/s , how many have v_x between -1m/s and 1m/s ?
- (d) Assume there is 1 mol of this gas in a rectangular container, and the total force exerted on one of the walls of the container by the gas is $9,000\text{N}$. Estimate the average time between 2 subsequent collisions of a given molecule with this wall. Assume the mean free path is much larger than the dimensions of this container.

Problem 3 (10 pts)

The Young modulus of concrete is $E=20\times 10^9\text{N/m}^2$. That means that to change the length of a concrete block by a fraction x requires a force per unit area xE .

The density of concrete at 10°C is $2,300\text{ kg/m}^3$. The coefficient of linear thermal expansion of concrete is $12\times 10^{-6}\text{ }^{\circ}\text{C}^{-1}$.

- (a) What is the density of concrete at 50°C , in kg/m^3 ?
- (b) If you lay concrete blocks of length 3m and cross-sectional area 0.5m^2 next to each other at temperature 10°C , what will be the force per unit area on the blocks when the temperature is 50°C ?
- (c) If you want the force per unit area on the blocks not to exceed $3\times 10^6\text{N/m}^2$ when the temperature varies between 10°C and 50°C , and you lay the blocks when the temperature is 10°C , what minimum space (in mm) should you leave between the blocks?