Assume that your skin can be considered a blackbody. One can then use Wien's displacement law, $\lambda_{\text{max}}T = 0.289~8 \times 10^{-2}~\text{m} \cdot \text{K}$ with $T = 35~^{0}\text{C} = 308~\text{K}$ to find

$$\lambda_{max} = \frac{0.289~8 \times 10^{-2}~\text{m} \cdot \text{K}}{308~\text{K}} = 9.41 \times 10^{-6}~\text{m} = 9~410~\text{nm} \; .$$

3-4 (a) From Stefan's law, one has $\frac{P}{A} = \sigma T^4$. Therefore,

$$\frac{P}{A} = (5.7 \times 10^{-8} \text{ W/m}^2 \text{ K}^4)(3000 \text{ K})^4 = 4.62 \times 10^6 \text{ W/m}^2.$$

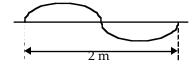
(b)
$$A = \frac{P}{4.62 \times 10^6 \text{ W/m}^2} = \frac{75 \text{ W}}{4.62 \times 10^6 \text{ W/m}^2} = 16.2 \text{ mm}^2.$$

- 3-5 (a) Planck's radiation energy density law as a function of wavelength and temperature is given by $u(\lambda, T) = \frac{8\pi hc}{\lambda^5 \left(e^{hc} / \lambda_B T 1\right)}$. Using $\frac{\partial u}{\partial \lambda} = 0$ and setting $x = \frac{hc}{\lambda_{\max} k_B T}$, yields an extremum in $u(\lambda, T)$ with respect to λ . The result is $0 = -5 + \left(\frac{hc}{\lambda_{\max} k_B T}\right) \left(e^{hc} / \lambda_{\max} k_B T\right) \left(e^{hc} / \lambda_{\max} k_B T\right)^{-1}$ or $x = 5\left(1 e^{-x}\right)$.
 - (b) Solving for x by successive approximations, gives $x \approx 4.965$ or $\lambda_{\text{max}}T = \left(\frac{hc}{k_B}\right)(4.965) = 2.90 \times 10^{-3} \text{ m} \cdot \text{K}$.
- 3-7 (a) In general, $L = \frac{n\lambda}{2}$ where n = 1, 2, 3, ... defines a mode or standing wave pattern with a given wavelength. As we wish to find the number of possible values of n between 2.0 and 2.1 cm, we use $n = \frac{2L}{\lambda}$

$$n(2.0 \text{ cm}) = (2)\frac{200}{2.0} = 200$$

 $n(2.1 \text{ cm}) = (2)\frac{200}{2.1} = 190$
 $|\Delta n| = 10$

As *n* changes by one for each allowed standing wave, there are 10 standing waves of different wavelength between 2.0 and 2.1 cm.



 $\left(\frac{1}{L}\right)\left(\frac{dn}{d\lambda}\right) = \frac{2}{\lambda^2}$. This gives approximately the same result as that found in (b): $\left(\frac{1}{L}\right)\left(\frac{dn}{d\lambda}\right) = \frac{2}{\lambda^2} = \frac{2}{\left(2.0 \text{ cm}\right)^2} = 0.5 \text{ cm}^{-2}$.

calculus to approximate $\frac{\Delta n}{L \Delta v} = \left(\frac{1}{L}\right) \left(\frac{dn}{d\lambda}\right)$. As $n = \frac{2L}{\lambda}$, $\left|\frac{dn}{d\lambda}\right| = \frac{2L}{\lambda^2}$ and

For short wavelengths n is almost a continuous function of λ . Thus one may use

For short wavelengths n is almost a continuous function of λ , $n = \frac{2L}{\lambda}$ is a discrete

The number of modes per unit wavelength per unit length is

 $\frac{\Delta n}{L\Delta \lambda} = \frac{10}{0.1} (200) = 0.5 \text{ cm}^{-2}$.

(b)

(c)

(d)

function.